

CSE547

Chapter 2, Problems 8

Chapter 2, Problem 8 Question.

What is the value of 0^m ,
when m is a given integer?

Chapter 2, Problem 8

Definition of $x^{\underline{m}}$ and $x^{\overline{m}}$

- $x^{\underline{m}} = x(x-1)\dots(x-m+1)$

From: (2.43) Concrete Mathematics
A Foundation for Computer Science
Graham, Knuth, Patashnik

- $x^{\overline{m}} = 1/[(x+1)(x+2)\dots(x+m)]$

From: Lecture Notes 9

Chapter 2, Problem 8

For $m \geq 1$

- For $m \geq 1$ we use the definition $x^m = x(x-1)\dots(x-m+1)$.
- $x = 0$ will always give us a product of 0.
$$0 = 0(0-1)\dots(0-m+1)$$

Chapter 2, Problem 8

For $m \leq 0$

- For $m \geq 1$ we use the definition $x^{-m} = 1/[(x+1)(x+2)\dots(x+m)]$.
- $0^{-m} = 1/[(0+1)(0+2)\dots(0+|m|)]$
 $= 1/[1*2*\dots*|m|]$
 $= 1/(|m|!)$

Chapter 2, Problem 8

Conclusion.

What is the value of 0^m ,
when m is a given integer?

0 , if $m \geq 1$;
 $1/(|m|!)$, if $m \leq 0$.