

Fractional Cascading in Wireless Sensor Networks

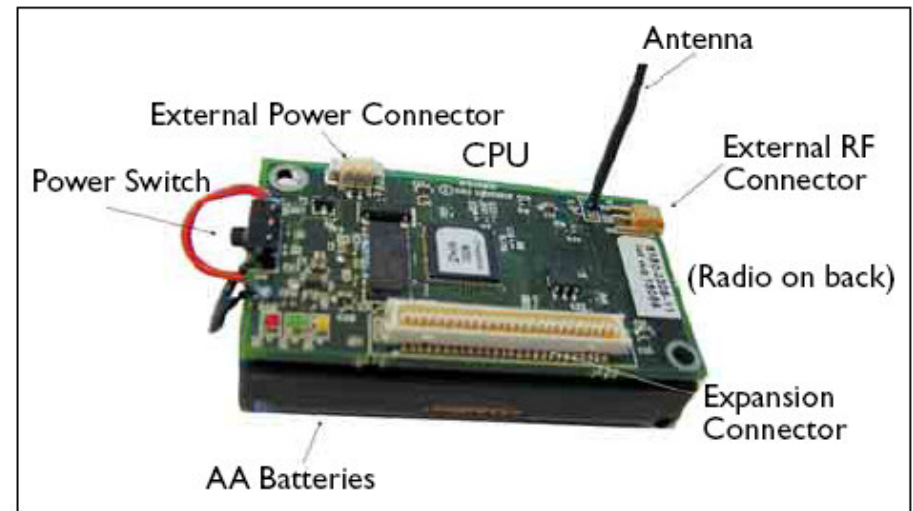
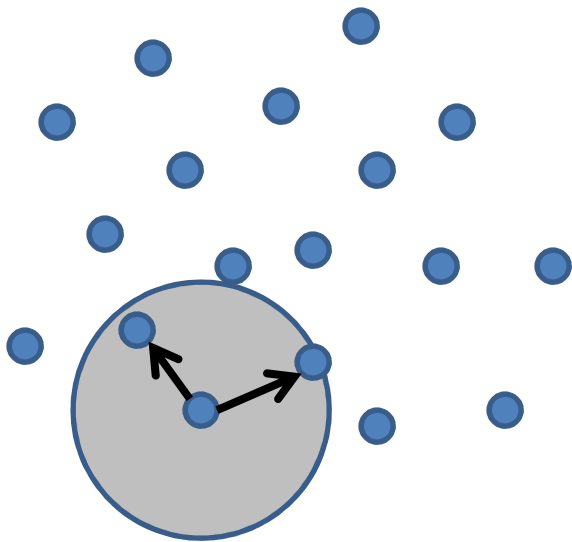
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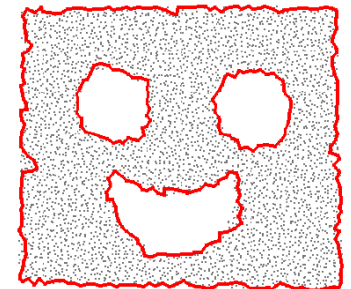
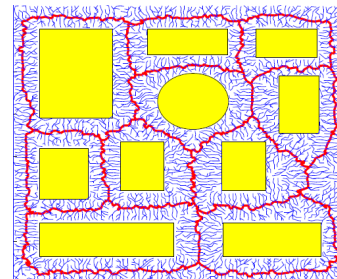
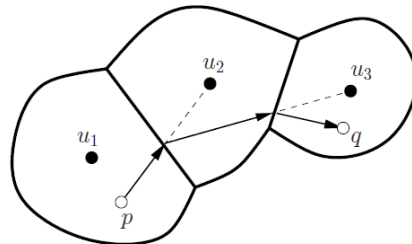
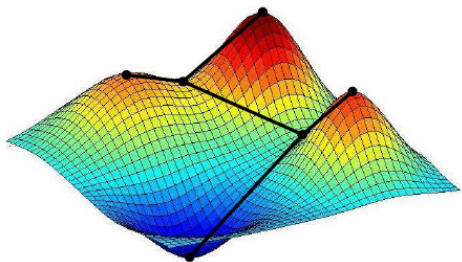
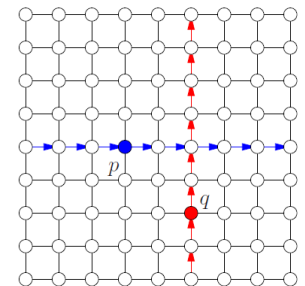
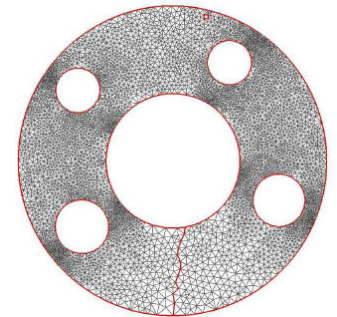
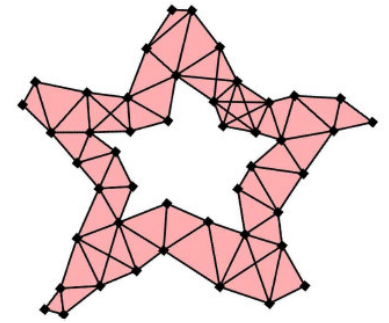
Sensor Networks

- Large number of small devices for environment monitoring



My recent work

- Lightweight, distributed algorithms
 - Routing
 - Network localization
 - Data aggregation/processing
 - Resource management
 - Network hole detection
 - Mobility issues

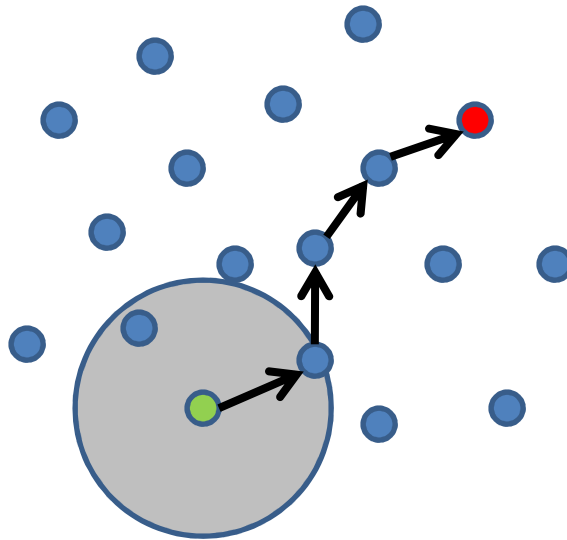


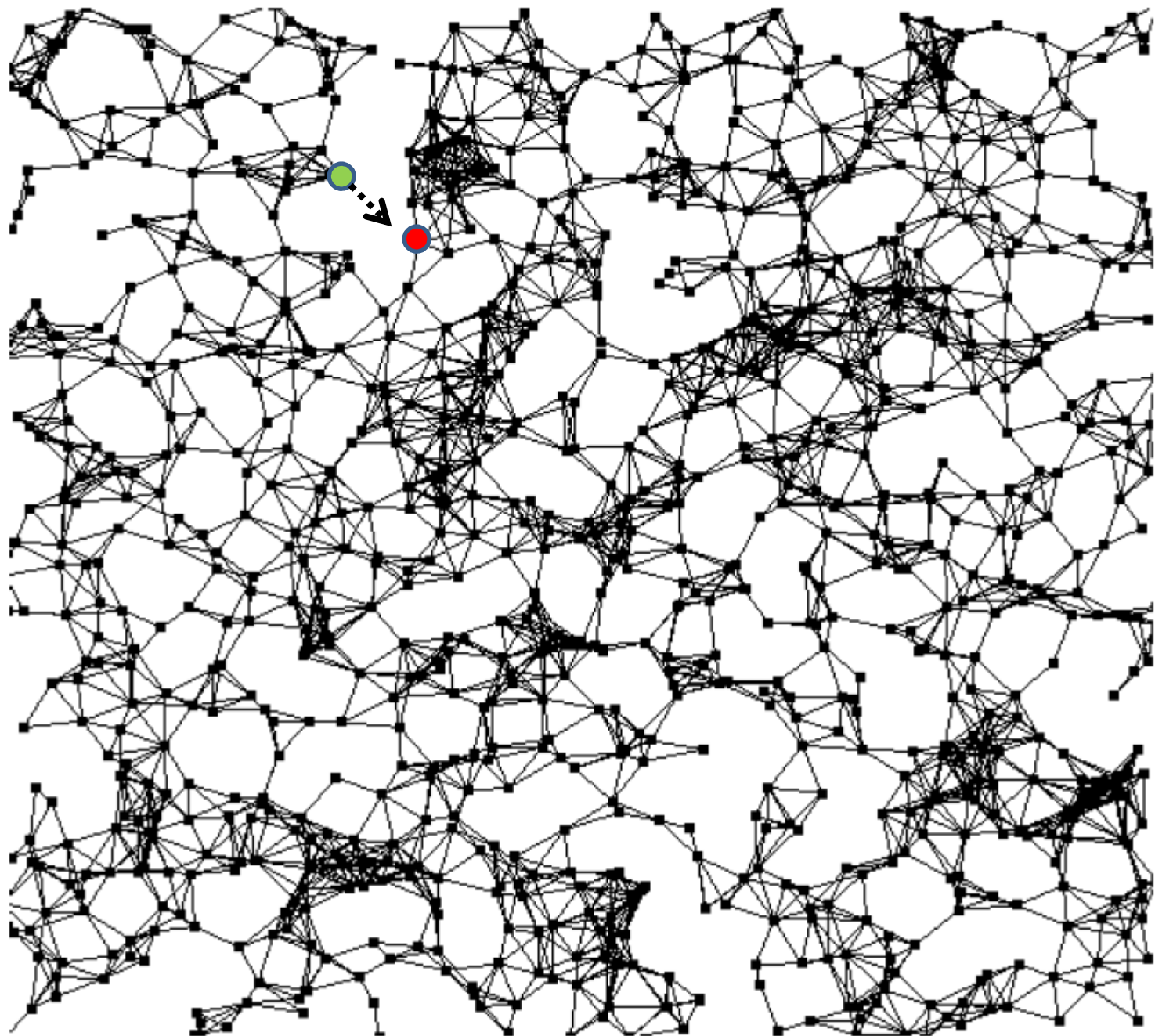
How much info should a node know about the network?

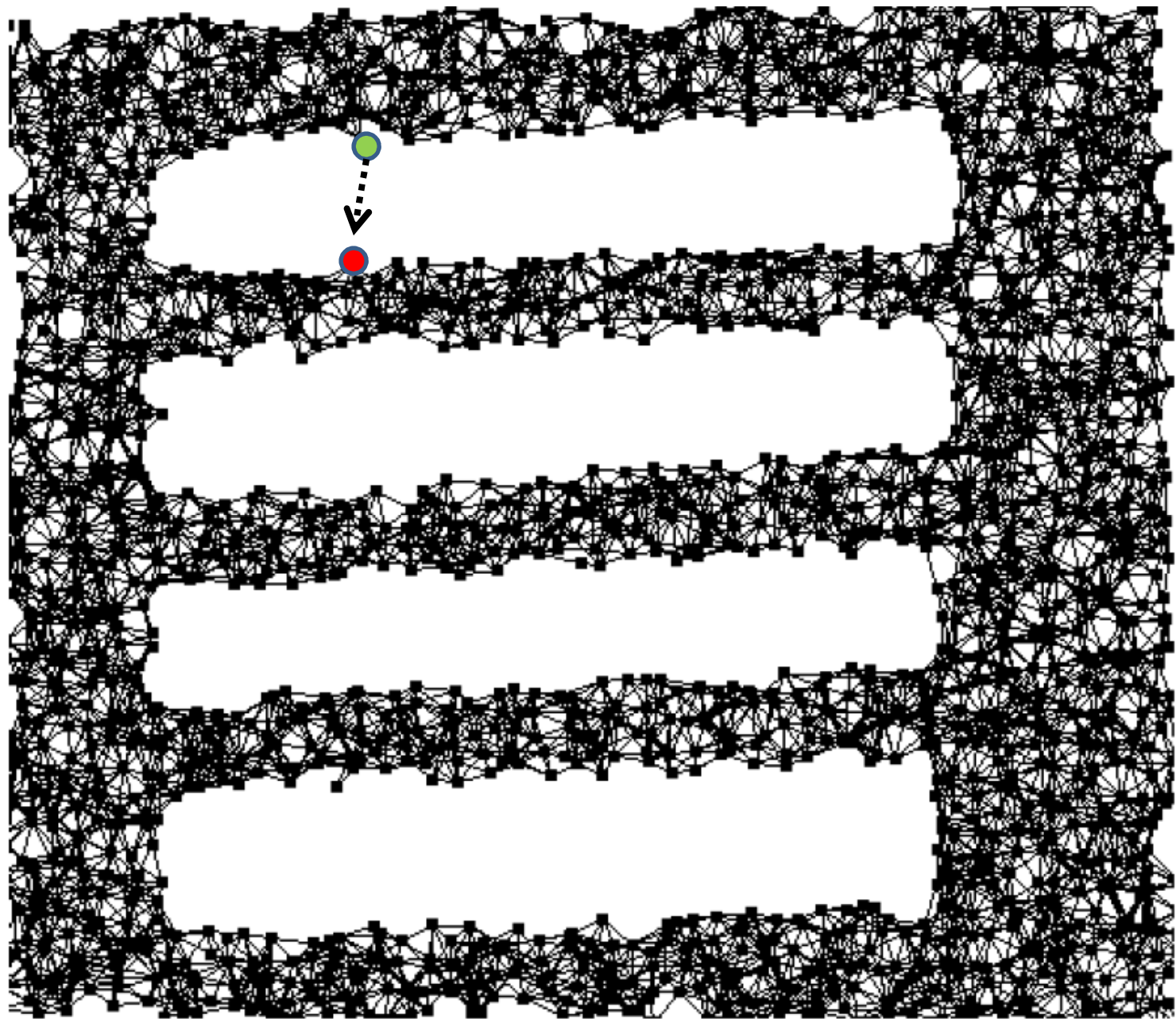
- Each node knows the entire network
 - Size of $O(n)$, not scalable
- Each node only knows its local neighbors
 - Difficult to achieve global objectives
- **Fractional cascaded information**: more knowledge of nearby nodes, less information of faraway nodes.
 - $O(\log n)$ size information
 - Support near optimal routing schemes.

Problem I: routing

- Find a near shortest path from s to t .
- Suppose each node knows the location of itself, its neighbors and the destination.
- Geographical greedy forwarding: send to a neighbor **closer** to the destination.

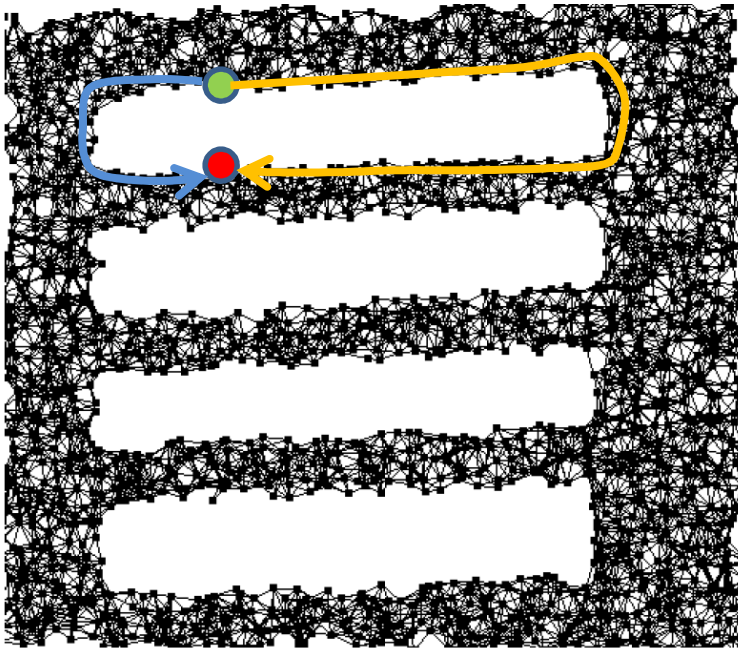






Routing local minimum

- A lot of literature on “how to get out of the local minimum.”
 - Most of them do not guarantee path quality.



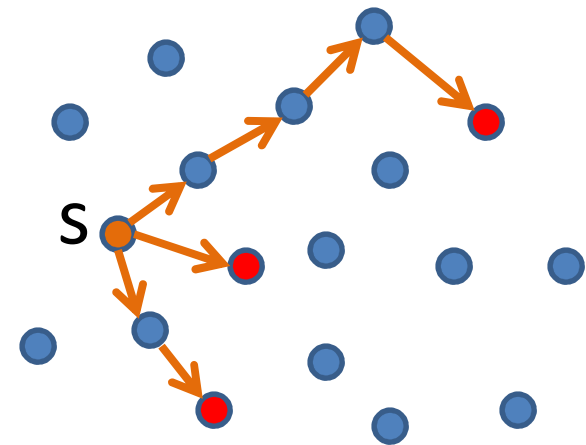
With only local information it is difficult to tell which path is shorter.

Routing local minimum

- The **geographical distance** $|st|$ is not an accurate measure of the **graph hop count distance** $\sigma(s, t)$.
- Our problem: given an **approximate distance oracle**, build routing tables s.t. some **greedy** method achieves **$1+\epsilon$** routing.
- Approach: each node stores paths to selected other nodes, called **long links**.
- Challenge: what long links to choose?

Build long links

- Each node build “long links” to all other nodes.
 - Achieves shortest path routing
 - Routing table size = $\Theta(n)$.
- Goal: select a few long links
 - Achieves $1+\epsilon$ routing.
 - Routing table size is $o(n)$.



What is next?

- I'll first explain a local algorithm for **routing in the plane**.
 - With Euclidean coordinates, how to route to a destination?
- Then extend to the case of sensor networks when
 - The Euclidean distance only **approximates** the (unknown) hop count distance.

An easier case: routing in the plane

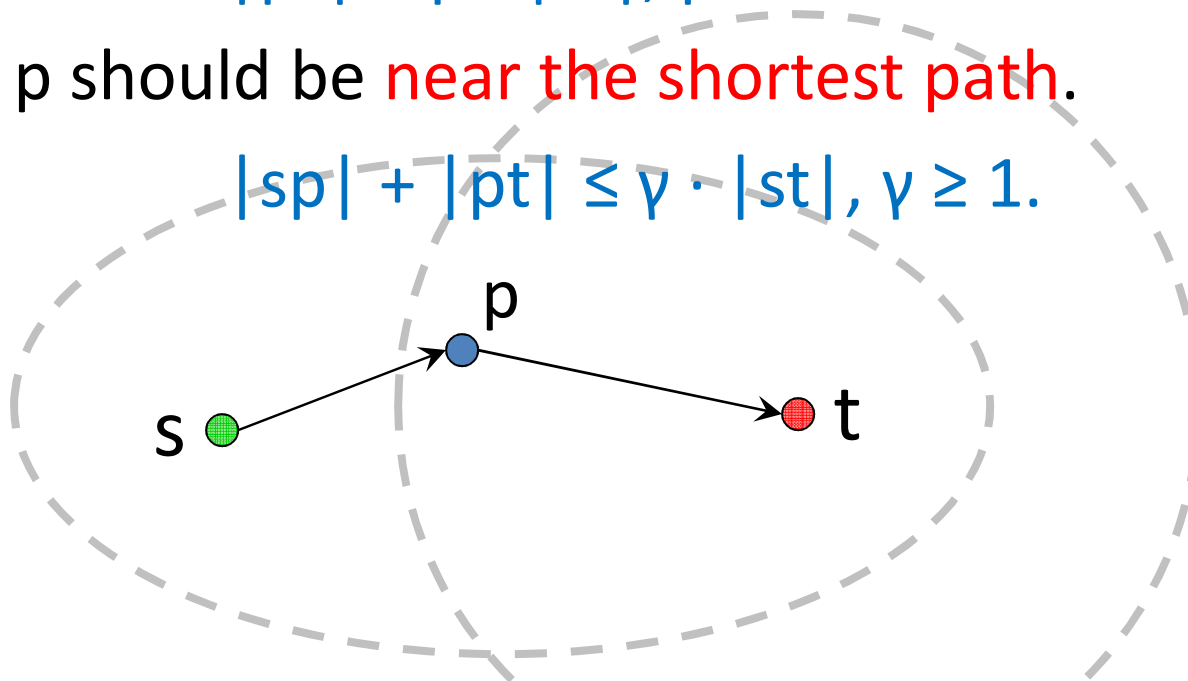
- Choose an intermediate node towards destination t

- p should be **closer to t**.

$$|pt| \leq \beta \cdot |st|, \beta \leq 1.$$

- p should be **near the shortest path**.

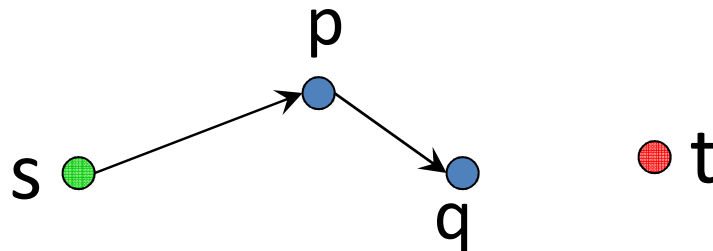
$$|sp| + |pt| \leq \gamma \cdot |st|, \gamma \geq 1.$$



Near shortest path routing

- Recursively, we get $1+\varepsilon$ path:

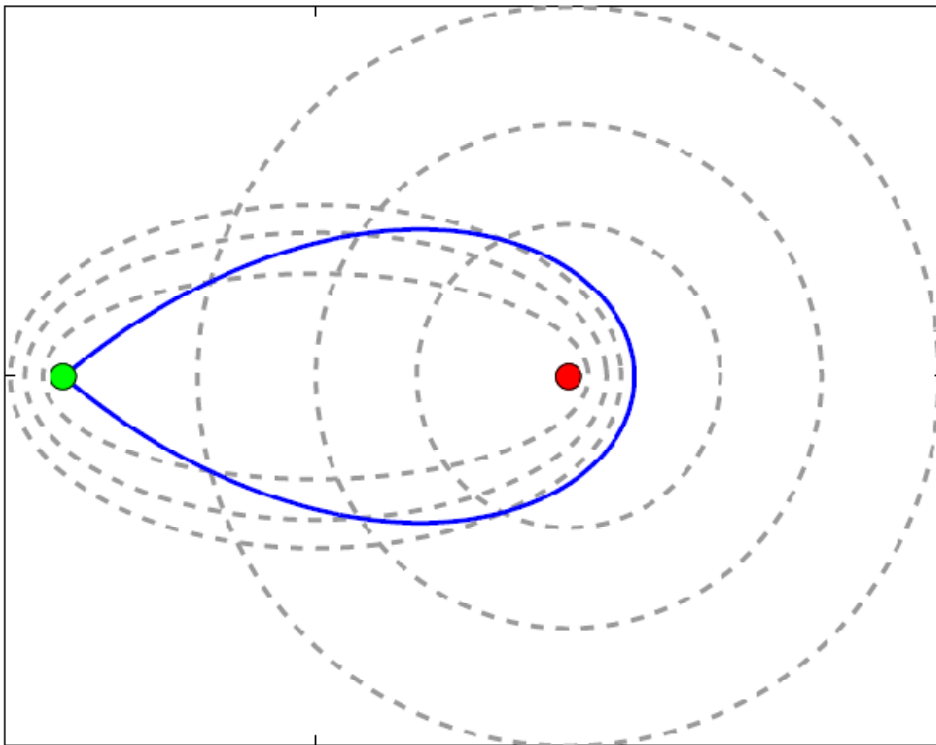
$$P(s, t) \leq (1+\varepsilon) \cdot |st|, \text{ if } (\gamma-1)/(1-\beta) \leq \varepsilon$$



- Only requirement: choose the next hop with the **forwarding region**.
 - $|pt| \leq \beta \cdot |st|, \beta \leq 1.$
 - $|sp| + |pt| \leq \gamma \cdot |st|, \gamma \geq 1.$

Forwarding region

- Near shortest path routing, if the next hop is within the forwarding region.

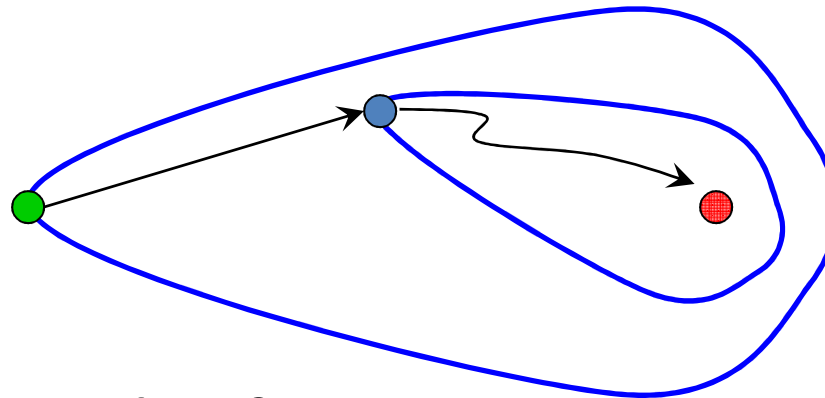


Boundary is defined by the intersection of
a ball: $|pt| \leq \beta |st|$ and
an ellipse: $|sp| + |pt| \leq \gamma |st|$

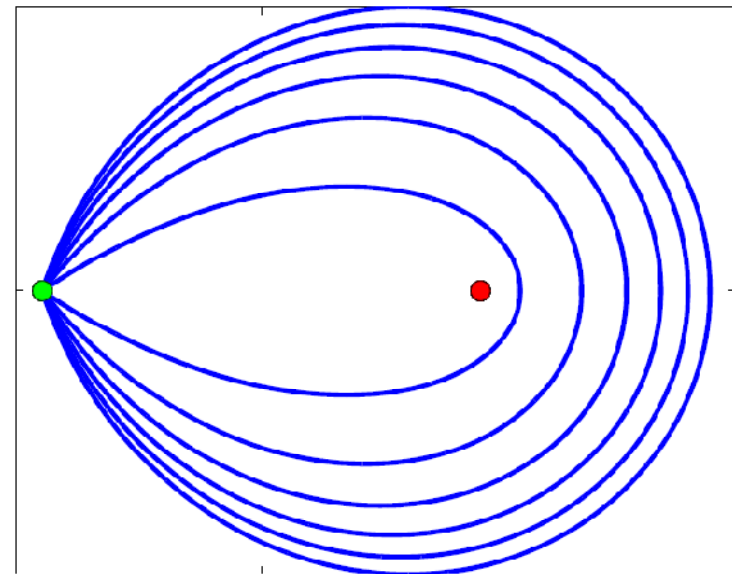
Local routing algorithm
achieving a global objective.

Forwarding region properties

- The shape of the forwarding region is scale invariant.



- The larger ε , the fatter.



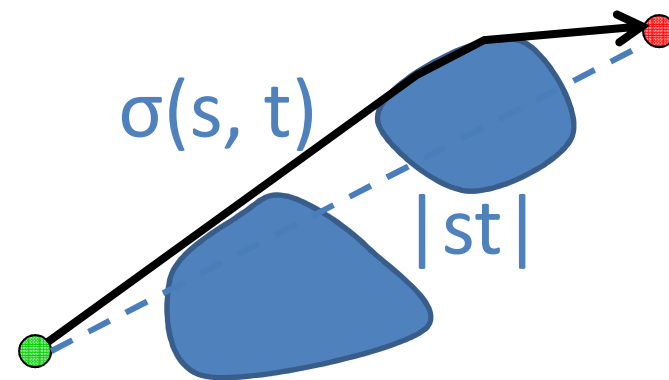
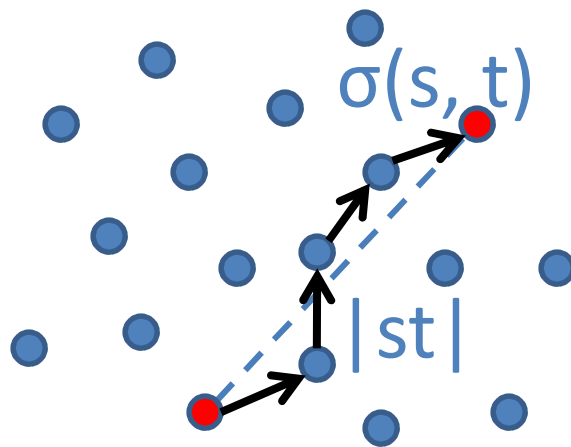
In the case of sensor networks

- Define forwarding region in the **graph** setting.
 - Replace Euclidean distance $|\cdot|$ by graph distance σ
 - Ball: $\sigma(\mathbf{p}, t) \leq \beta \cdot \sigma(s, t)$, $\beta \leq 1$.
 - Ellipse: $\sigma(s, \mathbf{p}) + \sigma(\mathbf{p}, t) \leq \gamma \cdot \sigma(s, t)$, $\gamma \geq 1$.
- Problem: graph distance σ is unknown.
 - Approximated by Euclidean distances.
 - Approximated by landmark-based distances.

[Kleinberg, Slivkins and Wexler, FOCS 04]

Euclidean distance = approximate distance oracle

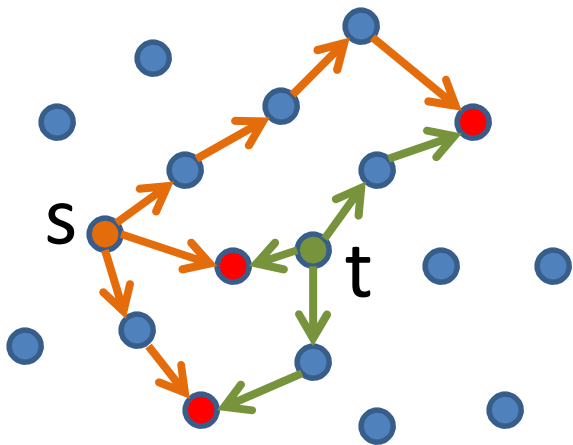
- Assumption: $\delta_1 |st| \leq \sigma(s, t) \leq \delta_2 |st|$, δ_1, δ_2 are two positive constants.
 - Local disturbances due to low sensor density
 - Global disturbances due to (fat) network holes



Landmark-based approximate distance oracle

- When Euclidean distances are not available
 - Each node measures hop counts to some landmarks L in the network
 - Use **triangle inequality** to bound $\sigma(s, t)$.

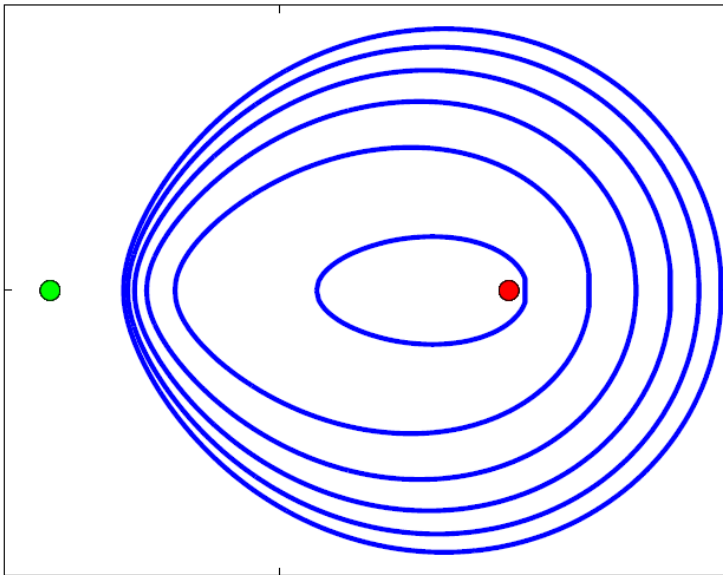
$$\max_j |\sigma(s, l_j) - \sigma(l_j, t)| \leq \sigma(s, t) \leq \min_j \sigma(s, l_j) + \sigma(l_j, t)$$



Kleinberg et.al. [FOCS 04] proved that with $O(\log n)$ landmarks this gives $1+\epsilon$ approximation for most pairs.

Forwarding region w/ approximate distance oracle

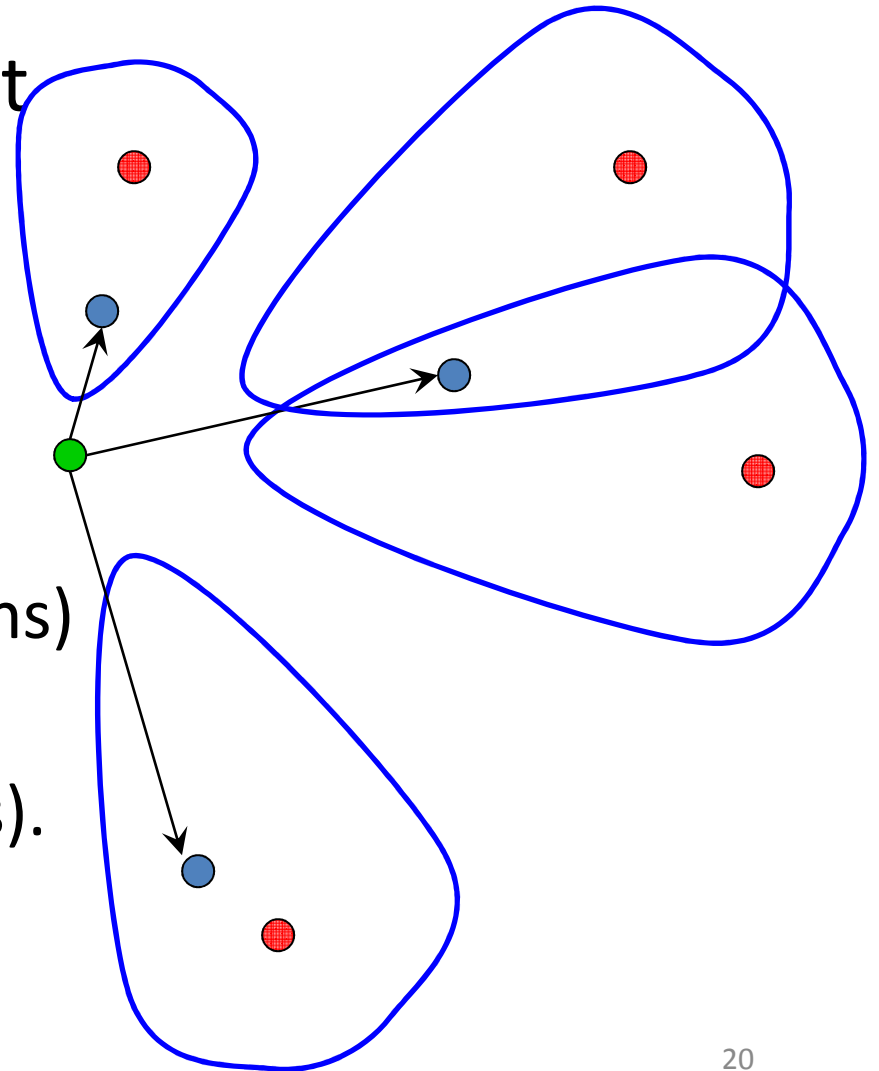
- Approximate distance $\delta_1 |st| \leq \sigma(s, t) \leq \delta_2 |st|$
 - Ball: $\delta_2 |pt| \leq \beta \cdot \delta_1 |st|$
 - Ellipse: $\delta_2 |sp| + \delta_2 |pt| \leq \gamma \cdot \delta_1 |st|$



- Smaller.
- Does not include source s.

Select long links in forwarding regions

- Select long links such that every forwarding region contains one link.
- Intuition:
 - select more links nearby (smaller forwarding regions)
 - and fewer links faraway (larger forwarding regions).



Solution: spatial distribution

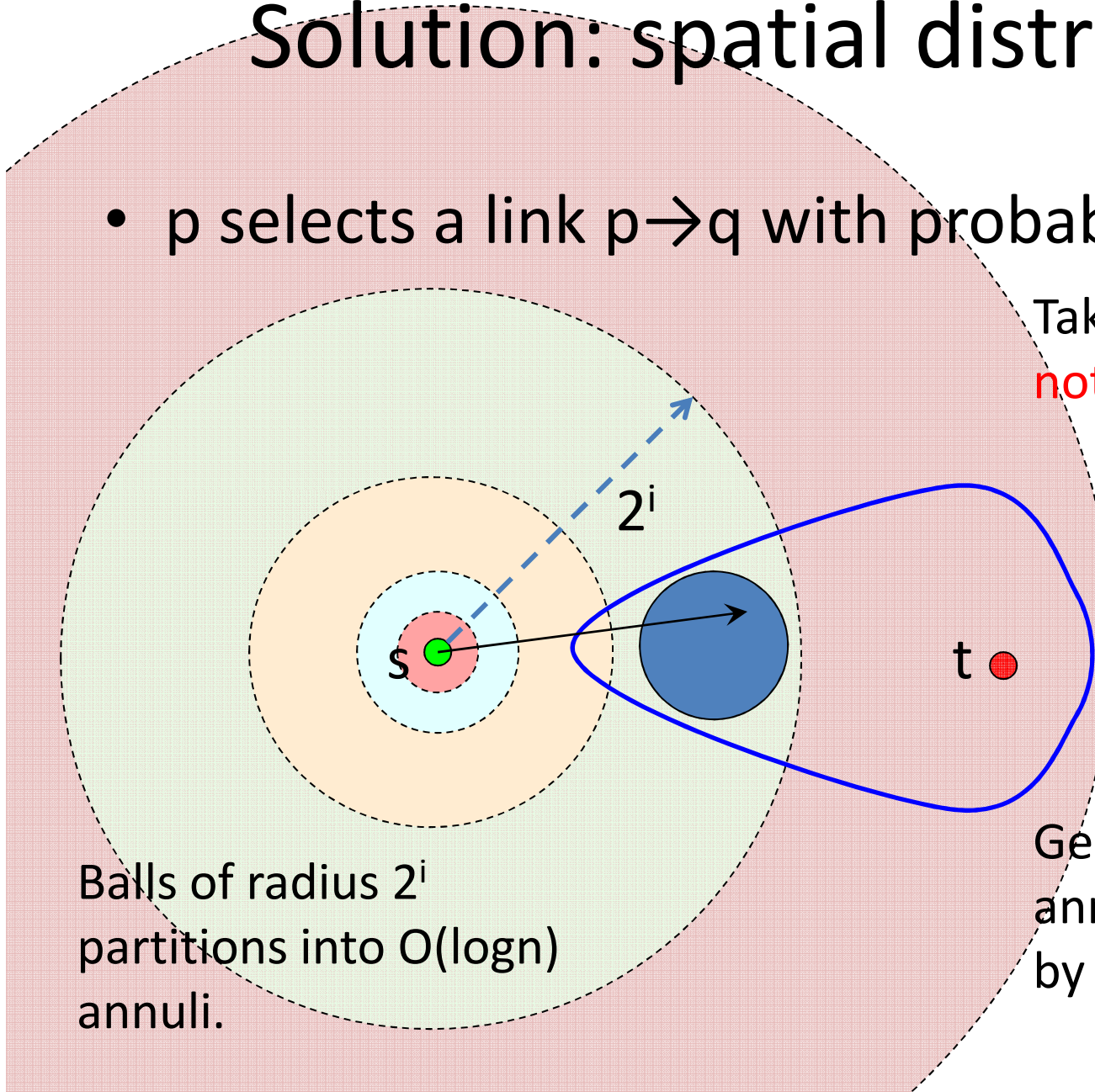
- p selects a link $p \rightarrow q$ with probability $\sim 1/|pq|^2$

Take the largest annulus **not** including t .

Inside this annulus there is a large ball $B \sim \Theta(|st|)$ inside the forwarding region.

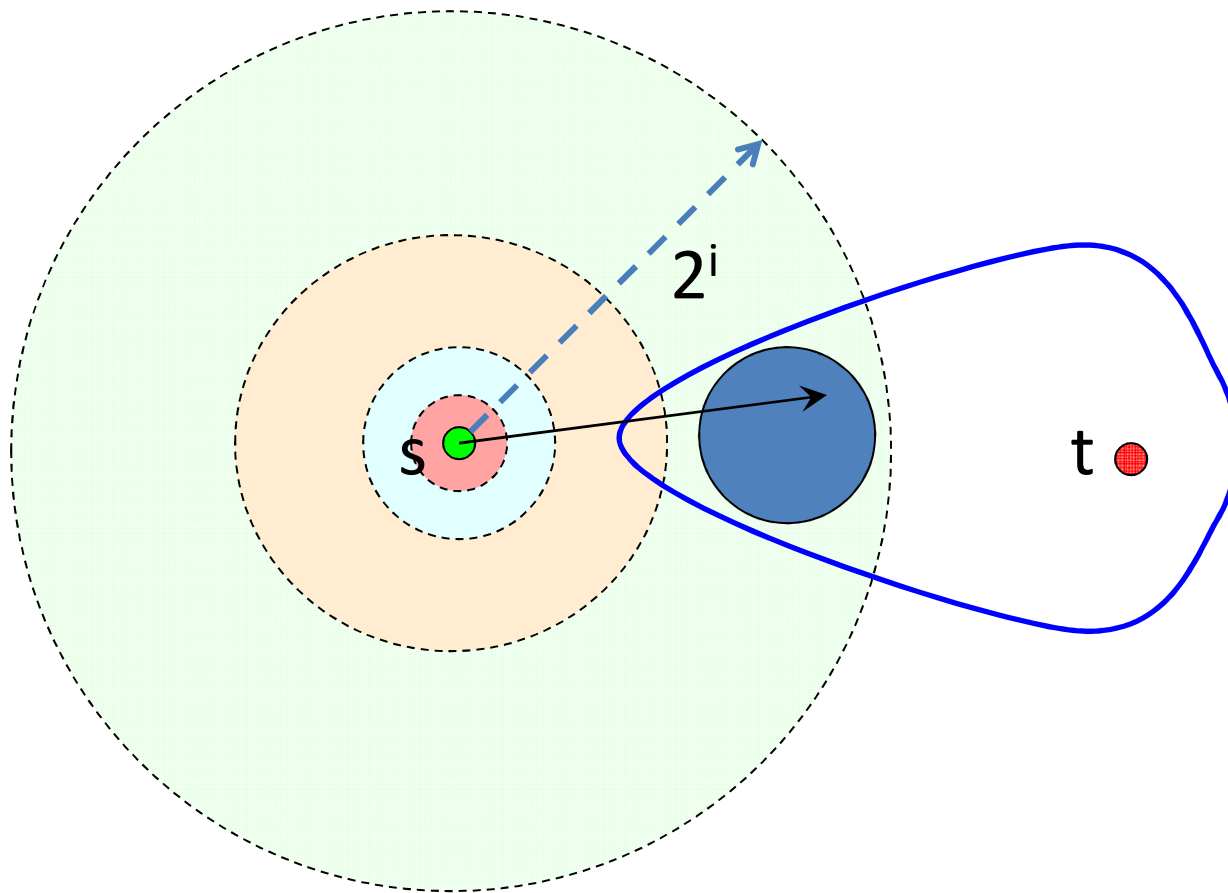
Geometric packing: Each annulus can be covered by $O(1)$ such balls.

Balls of radius 2^i partitions into $O(\log n)$ annuli.



Spatial distribution

- p selects a link $p \rightarrow q$ with probability $\sim 1/|pq|^2$

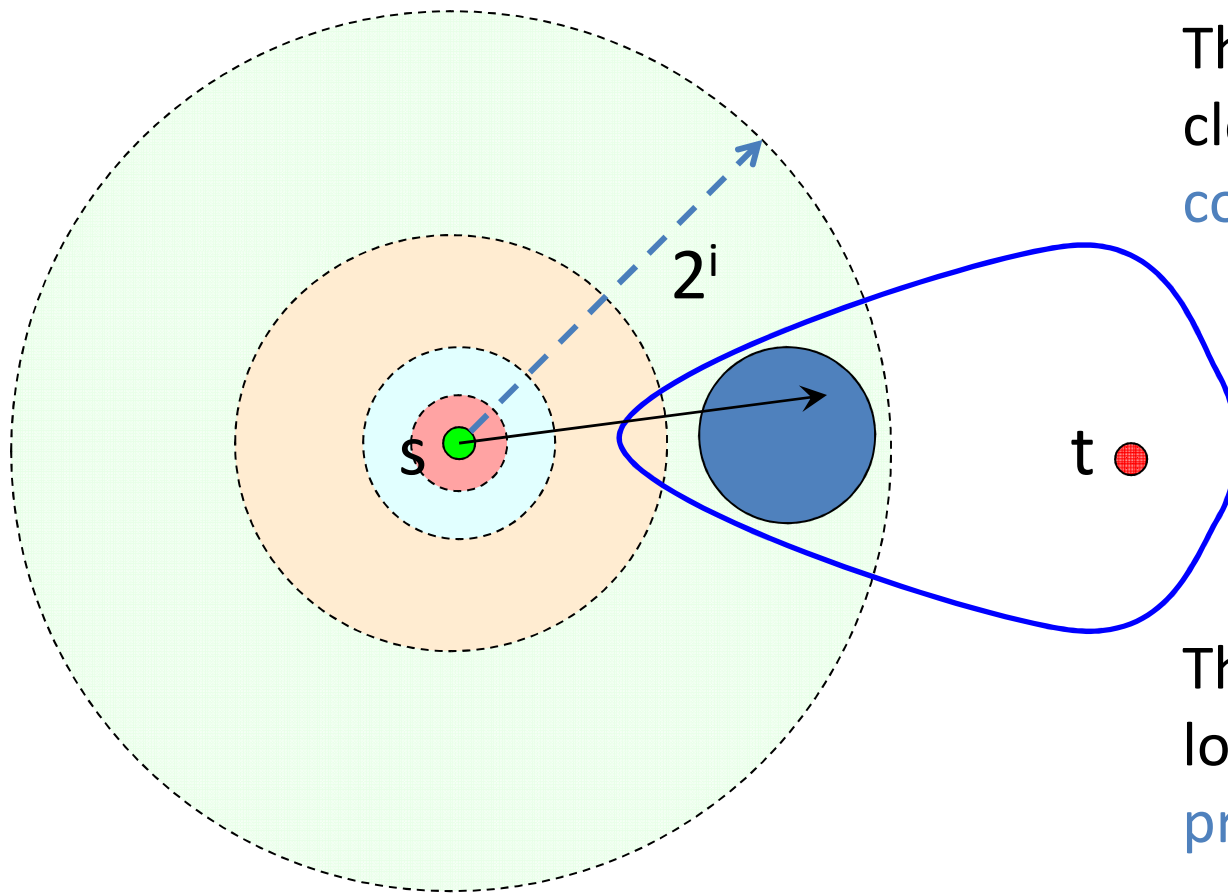


Each annulus has equal probability of getting a link. The ball B has prob $\sim 1/\log n$ of getting a link.

Balls and Bins: Select $O(\log^2 n)$ links such ball B has a long link with prob $\sim 1 - 1/n^2$

Routing path

- Routing path: put the long links together.



The first long link gets closer to t by a **constant** fraction.

The path consists of **$O(\log n)$** long links.

The path of $O(\log n)$ long links exists with **prob $\sim 1-1/n$** .

Graph setting

- Assumption: the graph has bounded growth rate \approx sensors are deployed w/ uniform density.
- # nodes of r hops away from $u = \Theta(r)$
- # nodes within r hops from $u = \Theta(r^2)$
- Similar packing argument holds.

Routing scheme put together

- Preprocessing:
 - Each node selects $O(\log^2 n)$ long links
 - The paths realizing these long links are stored at the routing tables of the nodes on the paths.
 - Randomized scheme, no global coordination.
- Routing:
 - Recursively select a long link in the forwarding region.
 - Local routing algorithm.

Select long links

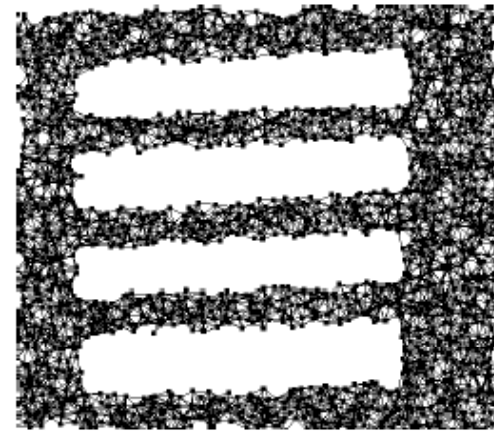
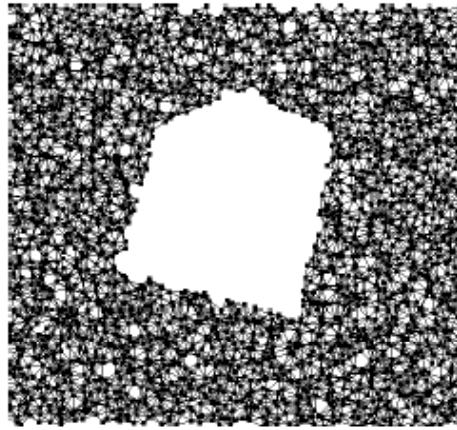
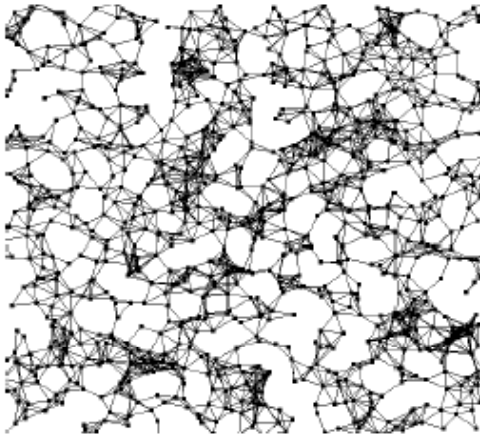
- Euclidean distance oracle
 - Sample a **point** with spatial distribution.
 - Round to the closest sensor **node**.
- Landmark-based distance oracle
 - $O(\log^2 n)$ random landmarks flood the network
 - Each node selects long links on the paths to these landmarks.

Construction of the routing tables

- Compute shortest paths
- Or, bootstrapping process:
 - All nodes first build the short “long links”
 - Use the short links to build longer “long links” (the same with standard routing operation)

Simulations

- Three topologies

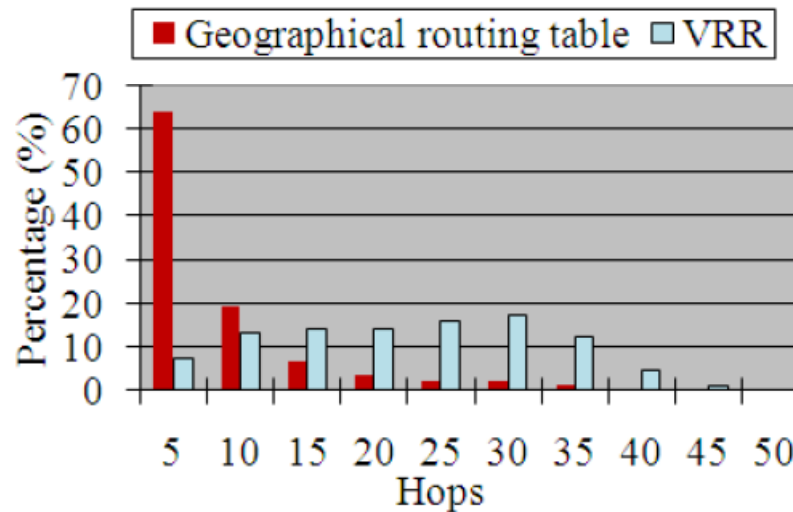


- Compare with

- **Virtual Ring Routing** (VRR): select long links uniformly randomly. [Caesar, et.al, SIGCOMM 06]
- **S4**: stretch-3 landmark-based routing (first route to the landmark closest to t, when getting close, use routing table). [Mao, et.al, NSDI 07]

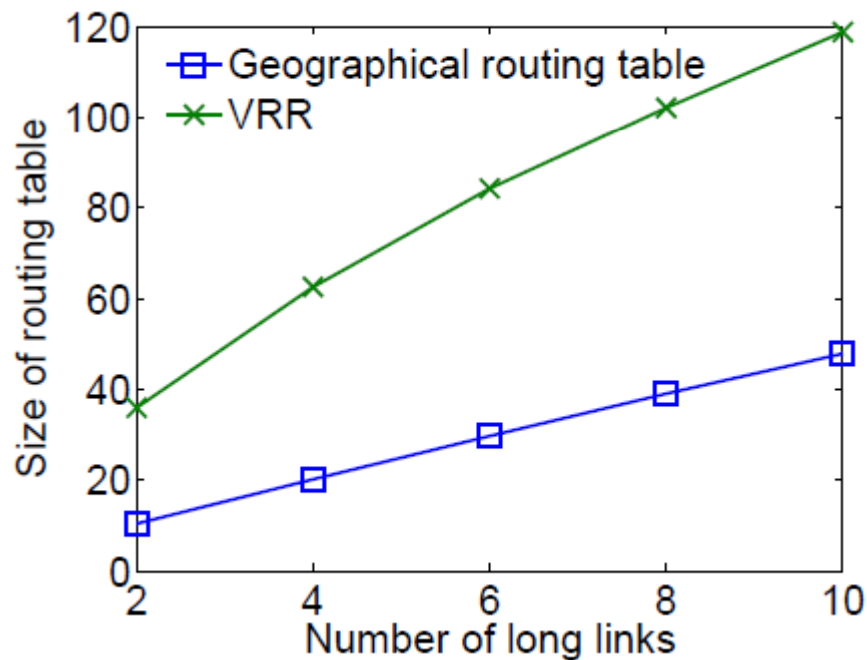
Our scheme v.s. VRR

- VRR: select randomly “long links”.
- We have smaller routing table, better stretch.

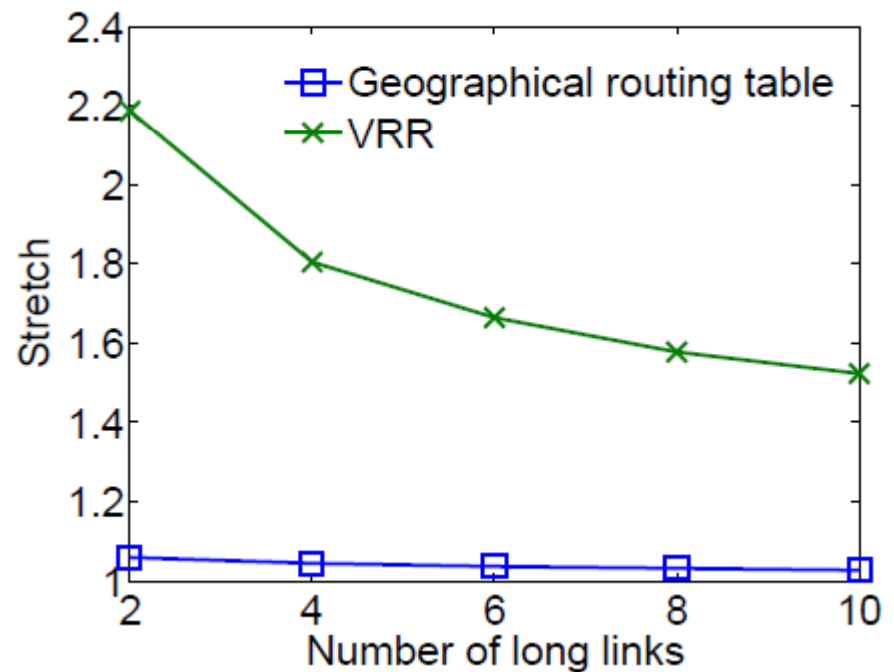


Our scheme v.s. VRR

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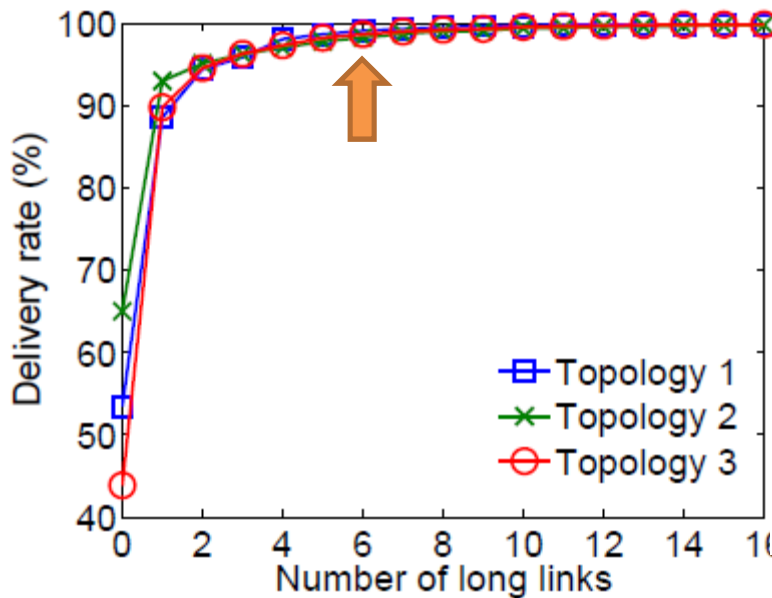
On average our “long links” are shorter.



Going “too far” hurts path stretch.

Routing stretch

- Comparable with S4 in stretch, with smaller routing table
- At a cost of small prob of delivery failure (i.e., need flooding)



↓

Average stretch	Our scheme	S4	VRR
Topology 1	1.03	1.03	1.73
Topology 2	1.03	1.03	1.80
Topology 3	1.04	1.02	1.75

↓

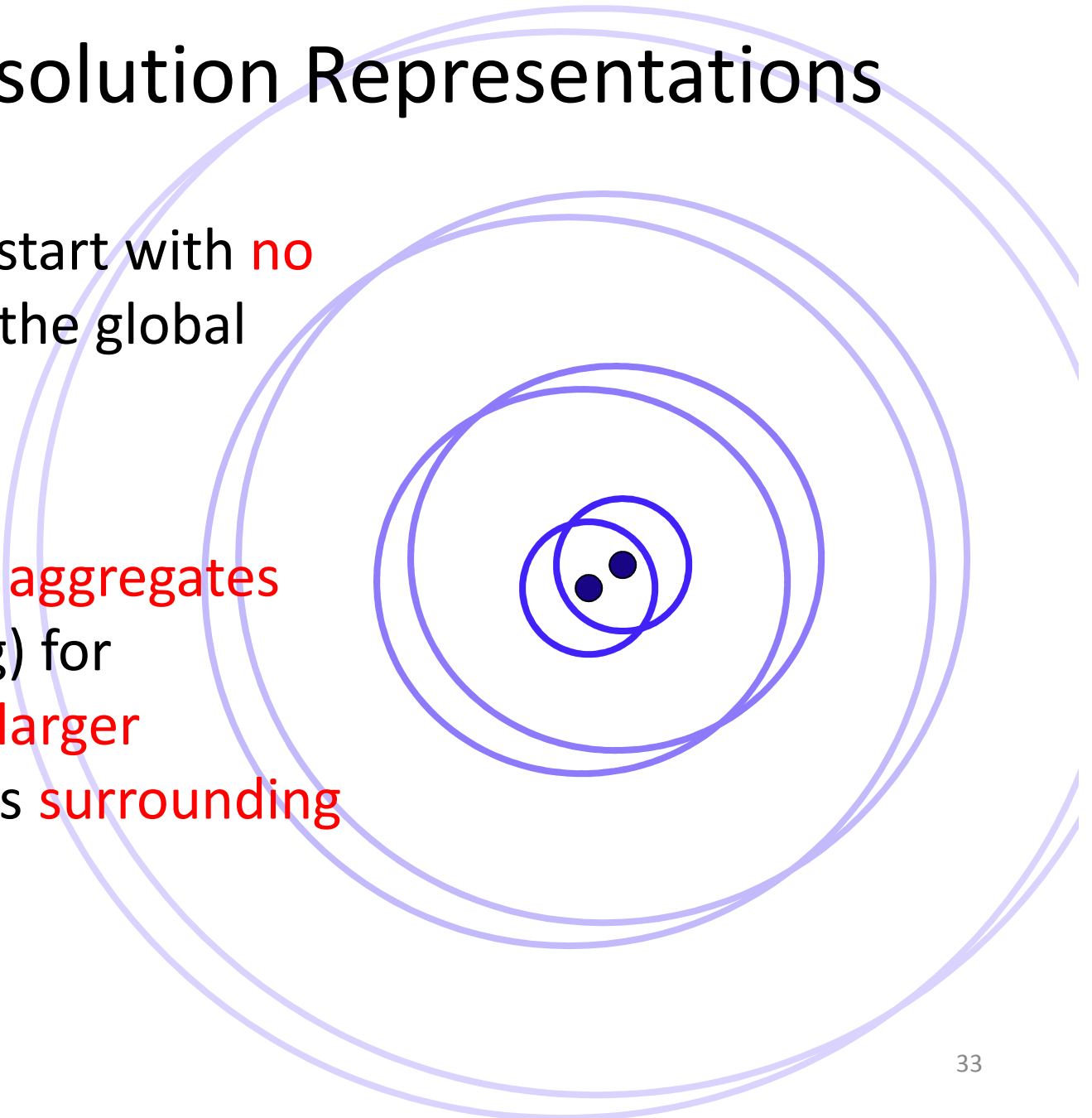
Size of routing table	Our scheme	S4	VRR
Topology 1	26.08	68.83	41.52
Topology 2	39.02	105.85	62.48
Topology 3	37.28	90.62	63.82

Summary of Part I

- Fractional cascaded information at each node to help routing.
- Strikes on scalability & locality while achieving globally optimal objectives.
- Part II: fractional cascaded information for data aggregation.

Multi-Resolution Representations

- Sensor nodes start with **no** knowledge of the global picture.
- Problem: Find **aggregates** (max, min, avg) for **exponentially larger** neighborhoods **surrounding each node**



Multi-resolutional data aggregation

- Each node keeps the aggregated information from all sensors within 2^i hops, $i=1, 2, \dots, \log n$.
 - Locally relevant picture of the network
 - Data validation (is it an outlier?)
 - Support range queries
- How to construct it?
- Flooding works, with total $\Theta(n^2)$ messages.
- Our solution: use **spatial gossip**.

Gossip algorithms

- In a round, each node:
 - Selects **another node** randomly
 - **Exchanges** information via multi-hop routing
 - Repeats every round
- Simple
- Distributed
- Robust to link dynamics, transmission errors

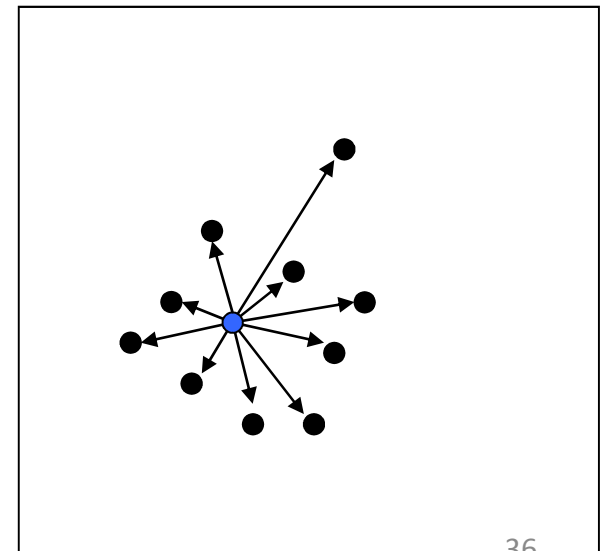
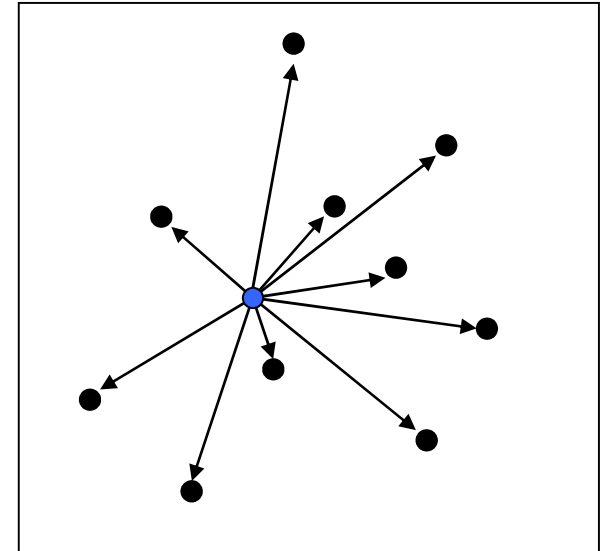
Types of Gossip

- Uniform/Geographic gossip
 - Select a node q **uniformly randomly** and gossip

[Dimakis, Sarwate, Wainwright, IPSN 06]

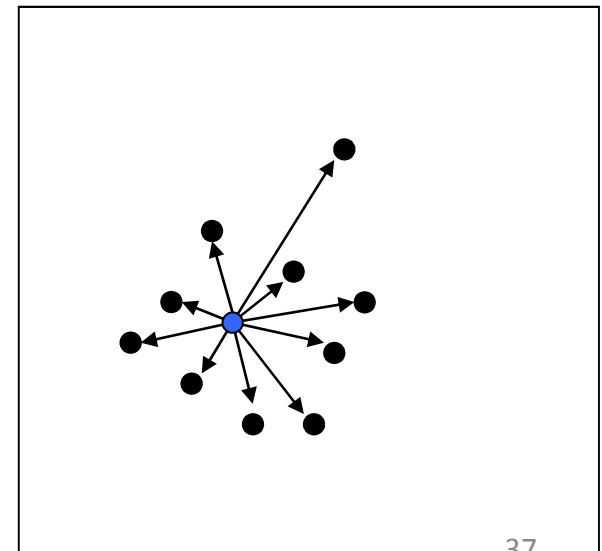
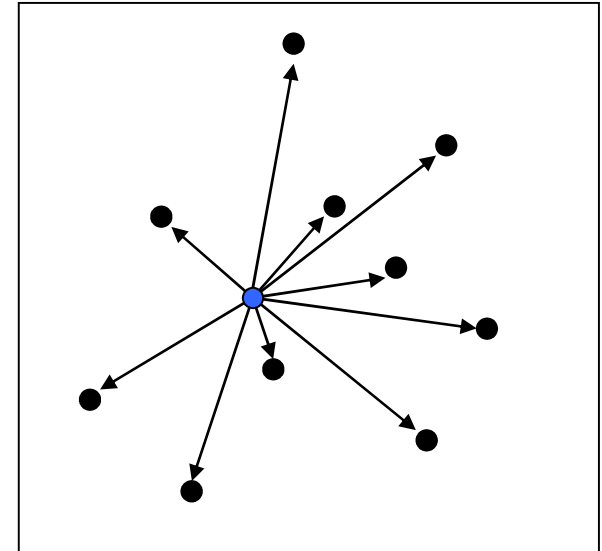
- Spatial Gossip
 - Select a node q at distance r with probability $1/r^\alpha$.

[Kempe, Kleinberg, Demers, STOC 01]



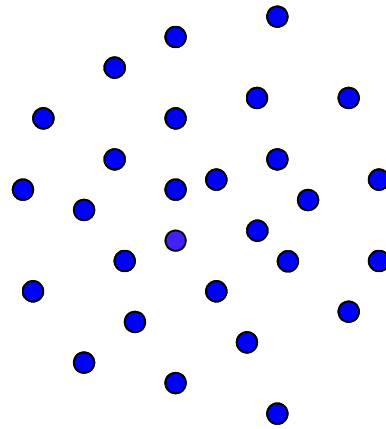
Communication Cost

- Uniform/Geographic gossip
 - Cost per step $\sim O(n\sqrt{n})$
 - # rounds for a message to reach everyone $\sim O(\log n)$
- Spatial Gossip
 - Prob= $1/r^2$, cost per step $\sim O(n\sqrt{n})$
 - Prob= $1/r^3$, cost per step $\sim O(n \log n)$
 - # rounds for a message to reach everyone $\sim O(\log n)$



Spatial Gossip

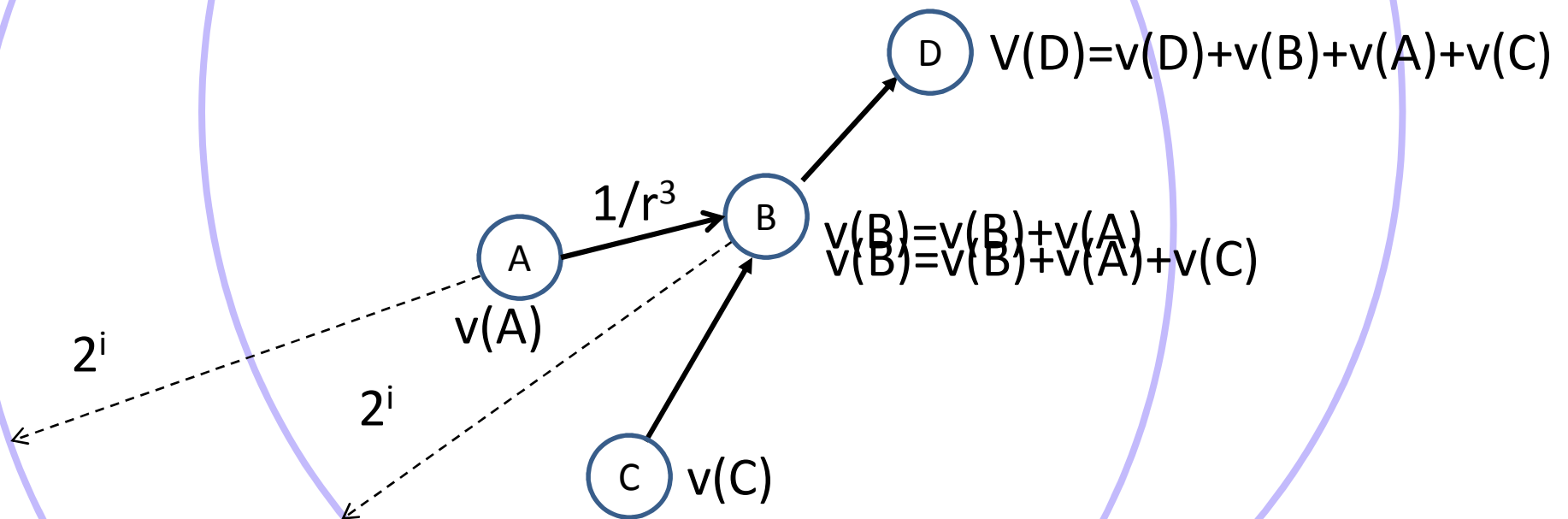
Expanding Neighborhood



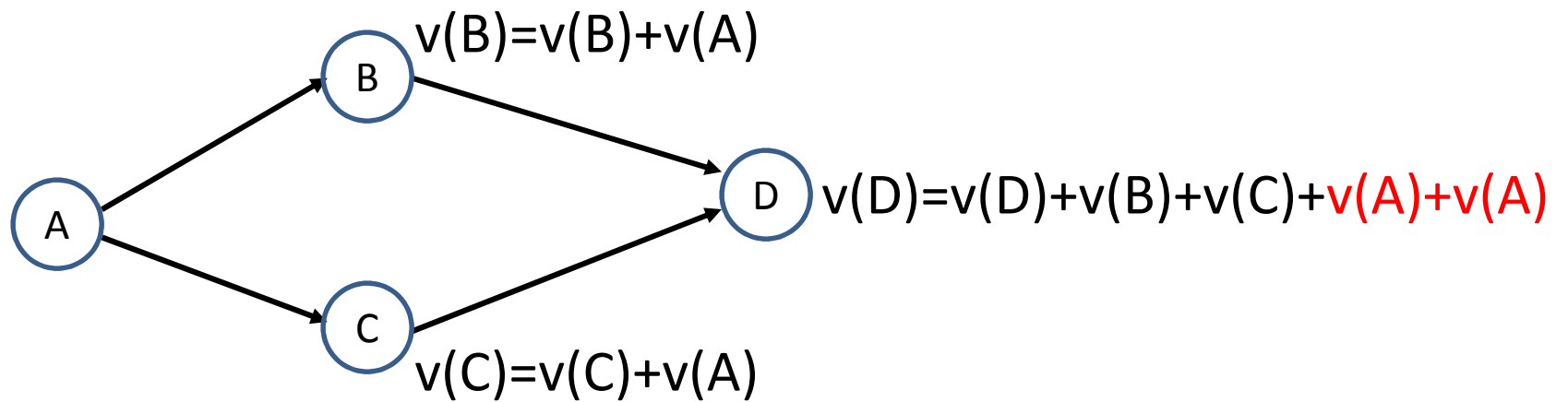
- Useful for multi-resolution aggregates

Using spatial gossip for aggregation

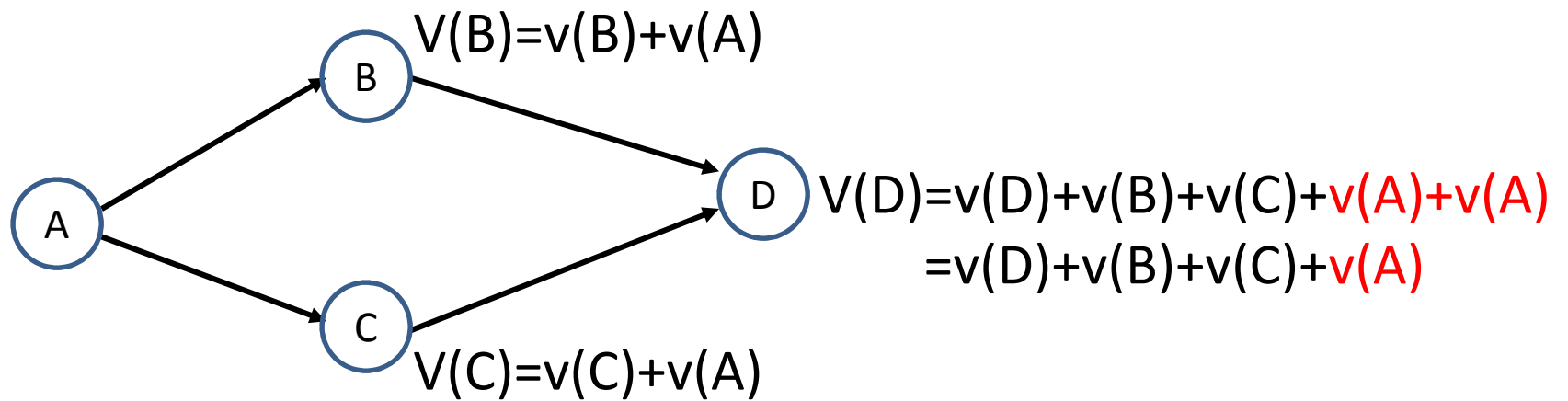
- Total $\log n$ phases
- In phase i we build aggregates for neighborhood of size 2^i around each node



Double counting?



Use Order and Duplicate Insensitive Aggregation



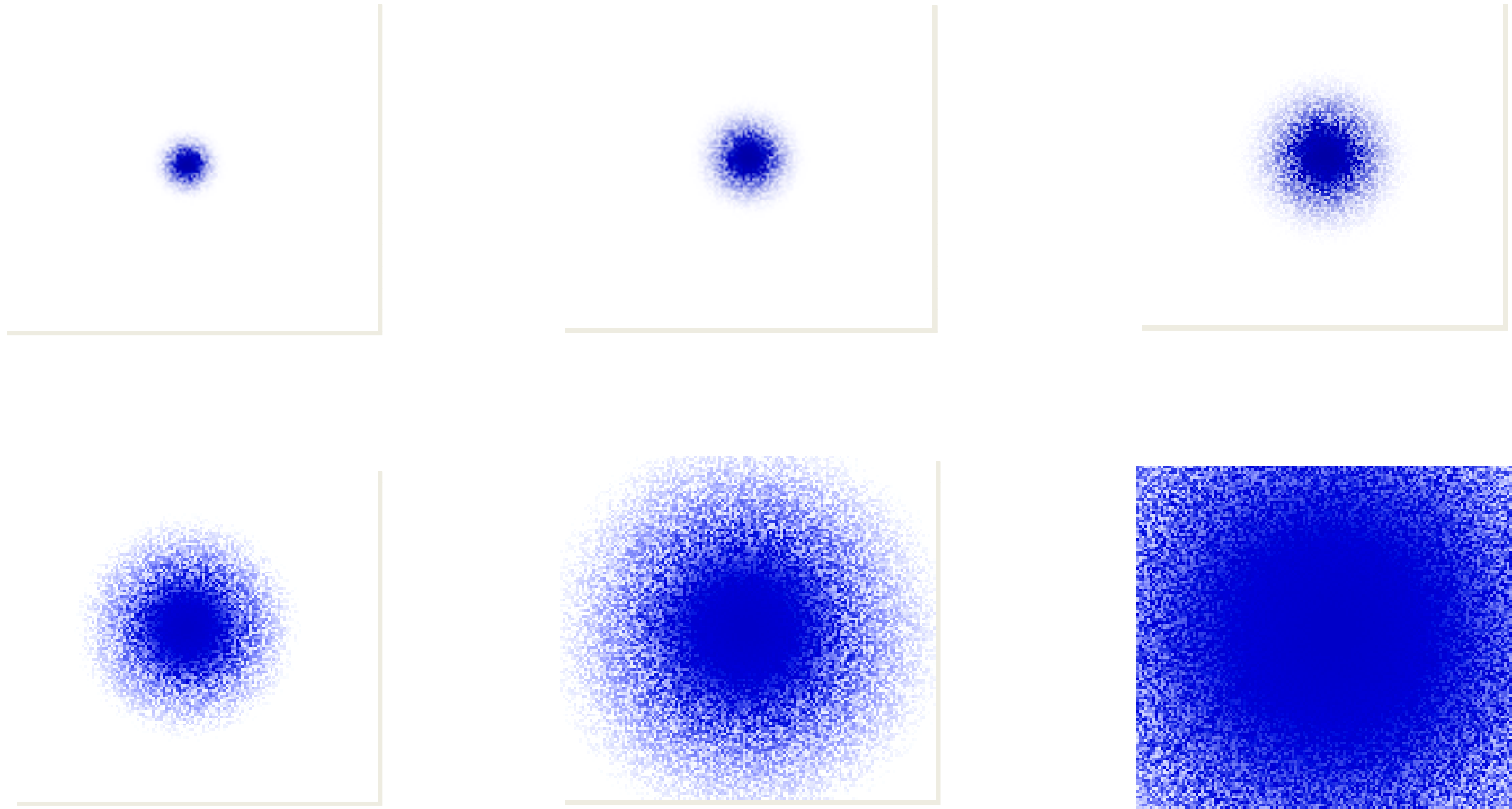
Order and Duplicate Insensitive Synopses

- The final aggregation does not change if a data value is aggregated multiple times.
- Min, Max are natural ODI aggregates
- ODI Synopses exist for other aggregates like sum, average, count..
 - Use probabilistic counting

Ref : Nath, Gibbons, Seshan, Anderson, SenSys 04

Considine, Kollios, Byers, ICDE 04

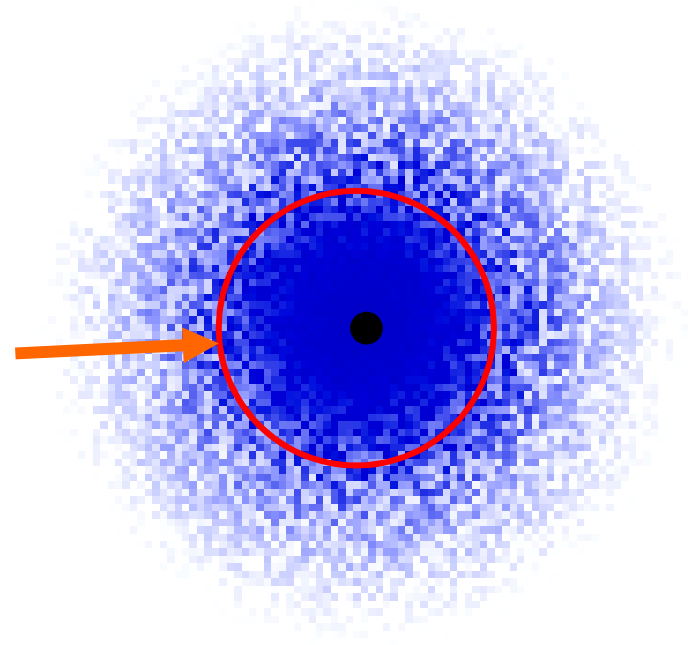
Data Distribution in Phases



Phases 1 to 6

Property 1 of Algorithm: Information Spreads Fast

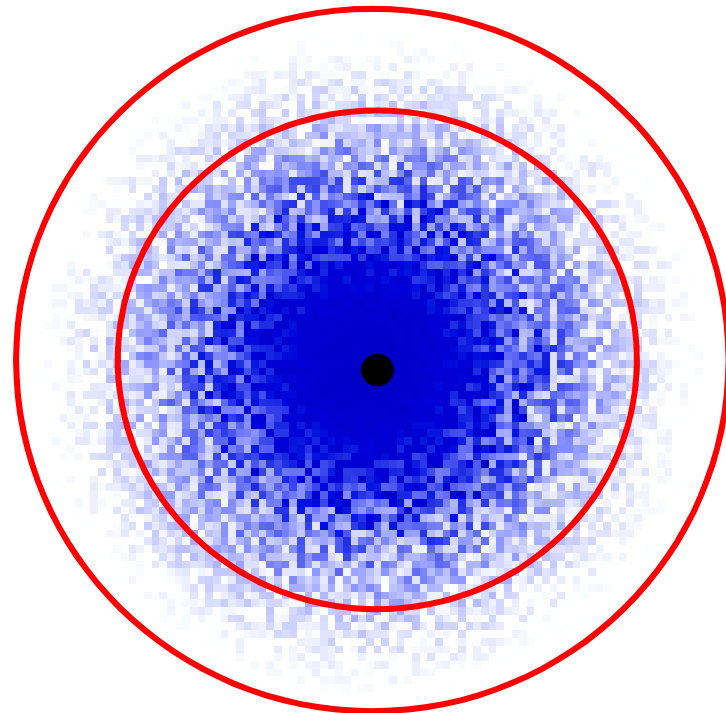
- In phase i , $i=1, 2, \dots, \log n$, with $O(i^{3.4})$ rounds, information spreads to every node within 2^i distance, with high probability.



Ref : Kempe, Kelenberg, Demers STOC 01

Property 2: Information Does Not Spread Too Far

- In phase i , $i=1, 2, \dots, \log n$, with $O(i^{3.4})$ rounds, information does not spread beyond distance $O(i^{3.4}2^i)$ for sure, and
- Does not spread beyond $O(i^{2.4}2^i)$ with high probability



Overall Efficiency

- $O(\log^{4.4}n)$ rounds.
- Total communication cost $O(n \log^{5.4}n)$.
- $O(\log n)$ aggregates per node simultaneously.

The Price of Accurate Computation

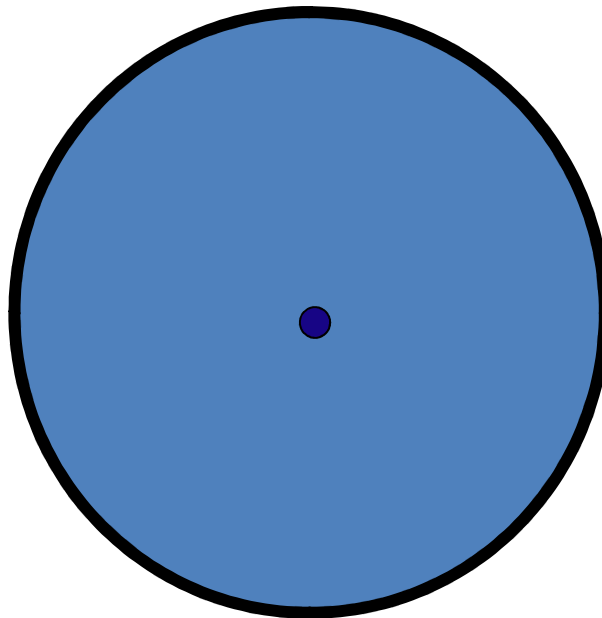
- Our aggregates are on **fuzzy** neighborhoods.
- **Sharp** multi-resolution aggregate computation requires a high communication cost of $\Omega(n\sqrt{n})$

Reduce the communication cost substantially by sacrificing a little on accuracy!

Range Queries

- User supplies a region, and asks for aggregate

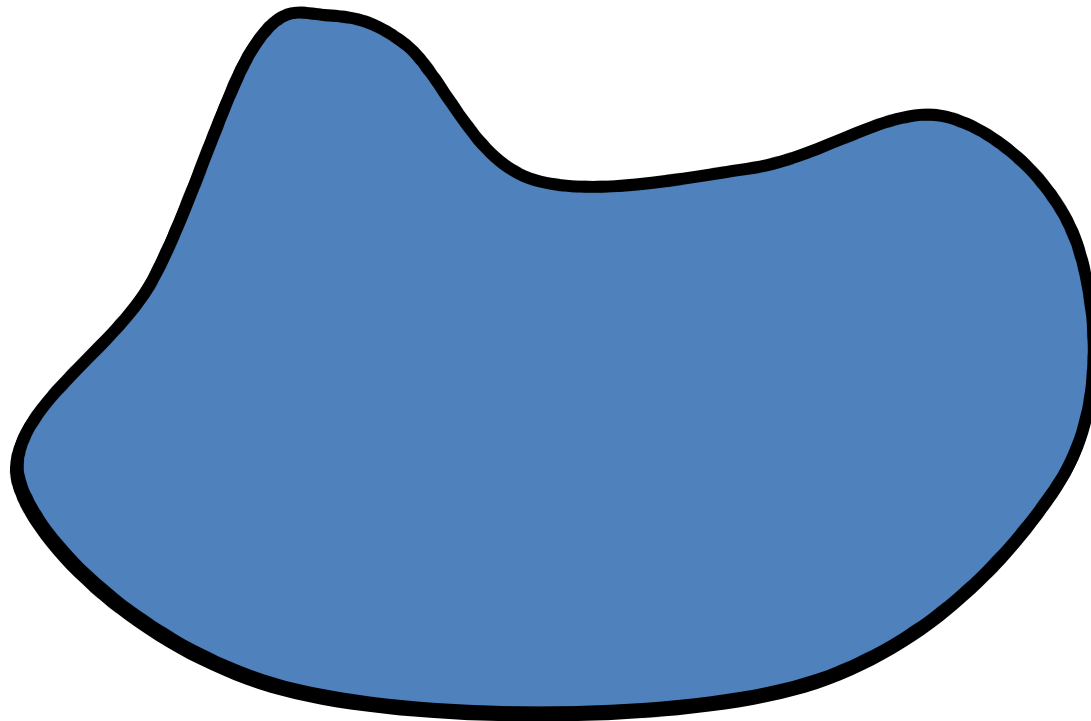
We pick a
suitable node



And a suitable
resolution
level to cover
the region

Range Queries

- Complex region
- Total communication cost \sim **perimeter**
- Cost of flooding \sim **area** of the region



Summary

- Information is most relevant in the spatial-temporal locale.
- Fractional cascading principle: diffuse information in a way cascaded with distances.
- Develop near optimal algorithms with low communication cost in a resource constrained network.

Questions or comments?

- Joint work with my students Rik Sarkar and Xianjin Zhu.
- Spatial distributions in routing table design for sensor networks, INFOCOM'09, mini-conference.
- Hierarchical spatial gossip for multi-resolution Representations in Sensor Networks, IPSN'07.
- Available at <http://www.cs.sunysb.edu/~jgao>