CSE508 Network Security



2021-03-11 **Public Key Cryptography**

Michalis Polychronakis

Stony Brook University

Public Key Cryptography

Many algorithms with different purposes

One common property: pair of keys, one public and one secret

Session key establishment

Exchange messages to create a shared secret key

Encryption

Anyone can encrypt a message using a recipient's public key
Only the recipient can decrypt a message using their private key
No shared secret! Private key (secret) is stored only at one side

Digital signatures

Sign a message with a private key

Diffie-Hellman Key Exchange

Allows two parties to jointly establish a shared secret key over an insecure communication channel

The established key can then be used to encrypt subsequent communication using a symmetric key cipher

"New Directions in Cryptography" by Whitfield Diffie and Martin Hellman, 1976

Based on the discrete logarithm problem

$$3^{29} \mod 17 \xrightarrow{easy} ??$$

$$3^{29} \mod 17 \xrightarrow{hard} 12$$

Diffie-Hellman Key Exchange

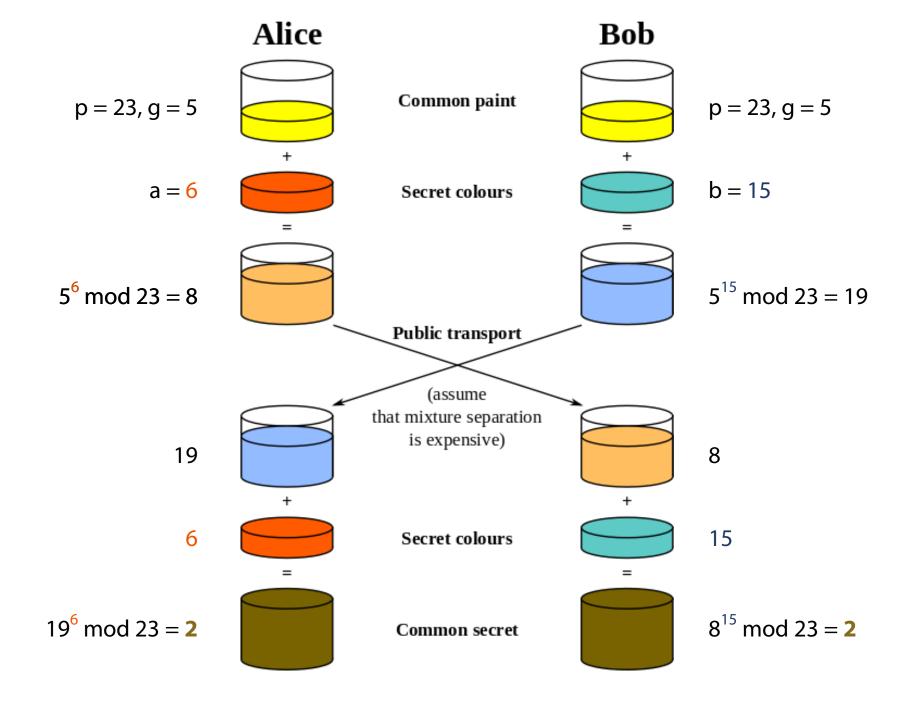
Alice and Bob agree on a large (at least 1024 bit) prime number p and a base $g-both\ public$

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p is usually of the form 2q+1 where q is also prime q is a generator of the multiplicative group of integers modulo p (for every q coprime to q there is a q such that q is also prime q to q there is a q such that q is also prime q is also prime q.
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Alice picks a secret large random number a and sends to Bob $g^a \mod p$ Bob picks a secret large random number b and sends to Alice $g^b \mod p$

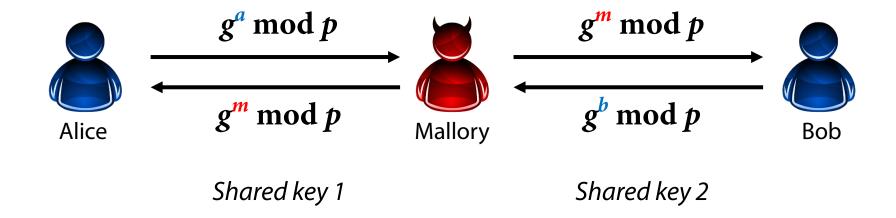
Alice calculates
$$s = (g^b \bmod p)^a = g^{ba} \bmod p$$

Bob calculates $s = (g^a \bmod p)^b = g^{ab} \bmod p$ shared key



Man-in-the-Middle Attack

Alice and Bob share no secrets

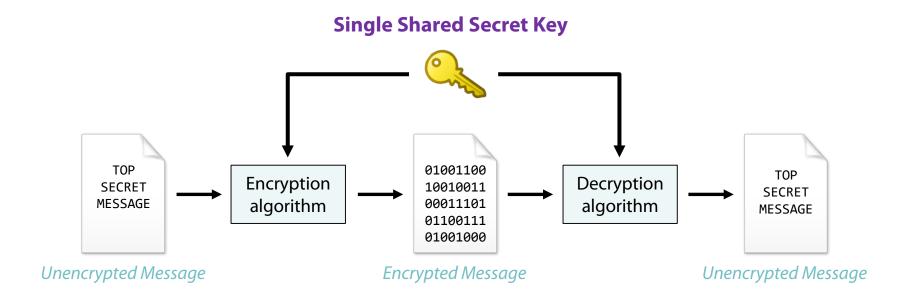


Mallory actively decrypts and re-encrypts all traffic

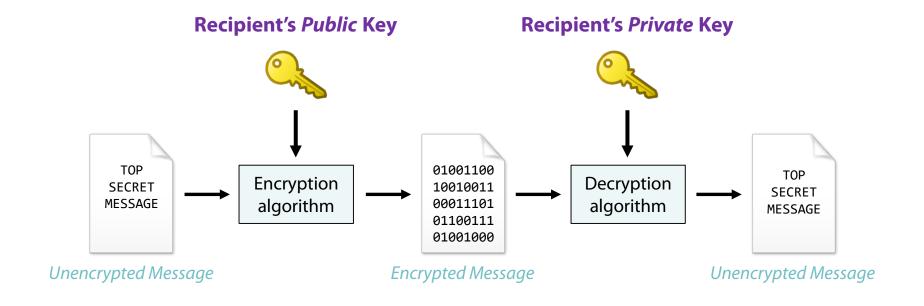
No authentication: Alice and Bob assume that they communicate directly

General problem: *need for a root of trust*

Symmetric Key Cryptography



Public Key Cryptography



Advantages

No shared secrets

Only private keys need to be kept secret, but they are never shared

Easier key management

No need to transmit any secret key beforehand

For *n* parties, *n* key pairs are needed (instead of n(n-1)/2 shared keys)

Provides both secrecy and authenticity

Disadvantages

More computationally intensive

Encryption/decryption is 2–3 orders of magnitude slower than symmetric key primitives

About one order of magnitude larger keys

Key generation is more difficult

RSA Asymmetric Encryption

Named after its inventors: Rivest, Shamir, Adleman

Based on the assumption that factoring large numbers is hard

Relatively easy to find two large prime numbers p and q

No efficient methods are known to factor their product N

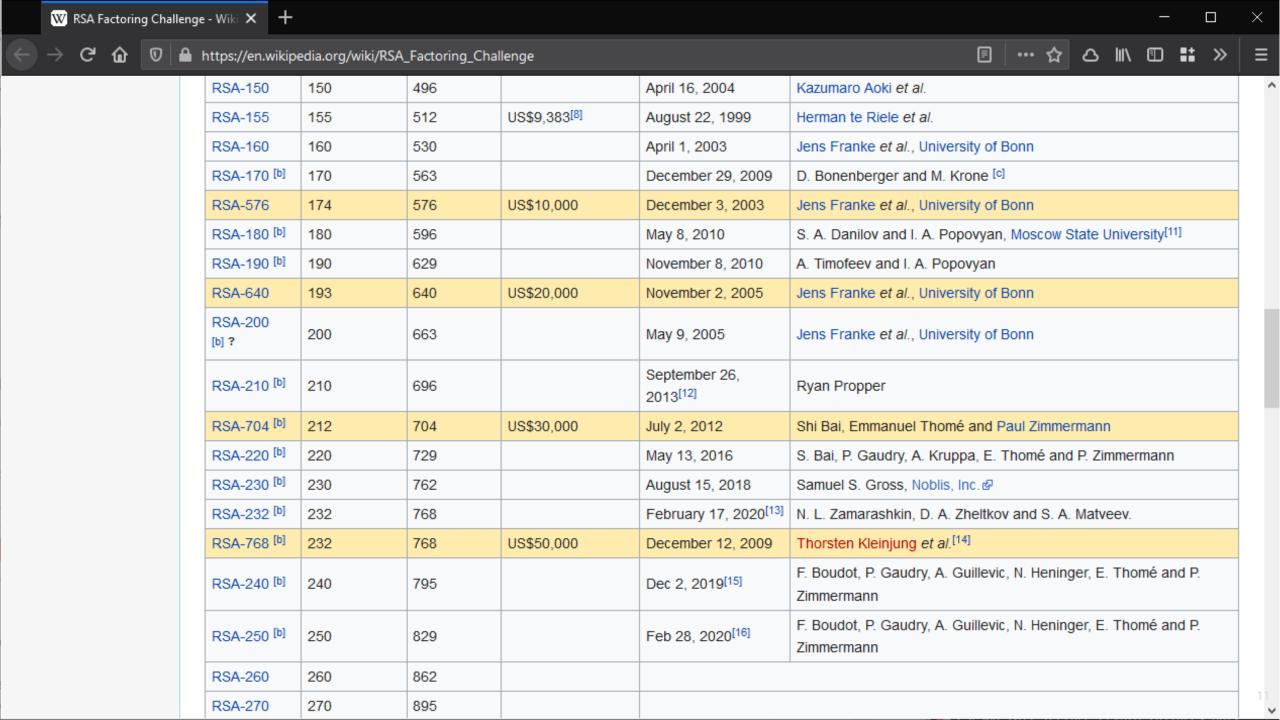
Variable key length

Largest (publicly known) factored RSA modulus is 768 795 829 bits long

February 2020: took roughly 2700 core-years

It is believed that 1024-bit keys may already (or in the near future) be breakable by a sufficiently powerful attacker

2048-bit keys should be the absolute minimum



RSA

Choose two distinct large prime numbers p and q

Let n = pq (modulus)

Select e as a relative prime to (p-1)(q-1)

Calculate d such that $de \equiv 1 \mod (p-1)(q-1)$

Public key = (e, n)

Private key = d

To encrypt m, calculate $c \equiv m^e \mod n$ Plaintext block must be smaller than the key length

To decrypt c, calculate $m \equiv c^d \mod n$ Ciphertext block will be as long as the key

RSA in Practice

RSA calculations are computationally expensive

Two to three orders of magnitude slower than symmetric key primitives → RSA is used in combination with symmetric key encryption

Sending an encrypted message:

Encrypt message with a random symmetric key

Encrypt the symmetric key with recipient's public key

Transmit both the encrypted message and the encrypted key

Setting up an encrypted communication channel:

Negotiate a symmetric key using RSA

Use the symmetric key for subsequent communication

PKCS: Public-Key Cryptography Standards (#1–#15)

Make different implementations interoperable

Avoid various known pitfalls in commonly used schemes

Forward Secrecy

Threat: capture encrypted traffic now, use it in the future

Private keys may be compromised later on (e.g., infiltrate system)

A cryptanalytic breakthrough may be achieved

FS: Even if current keys are leaked, past encrypted traffic cannot be decrypted

Generate random secret keys without using a deterministic algorithm

Cannot read old messages

Cannot forge a message and claim that it was sent in the past

Support

IPsec, SSH, Off-the-Record messaging (OTR), TLS (Diffie-Hellman instead of RSA key exchange)

Not a panacea

Ephemeral keys may be kept in memory for hours

Server could be forced to record all session keys

TLS session resumption needs careful treatment

Elliptic Curve Cryptography

Proposed in 1985, but not used until 15 years later

Relies on the intractability of a different mathematical problem: "elliptic curve discrete logarithm"

Main benefit over RSA: shorter key length

Example: a 256-bit elliptic curve public key is believed to provide comparable security to a 3072-bit RSA public key

Endorsed by NIST

Key exchange: elliptic curve Diffie–Hellman (ECDH)

Digital signing: elliptic curve digital signature algorithm (ECDSA)





Commercial National Security Algorithm Suite and Quantum Computing FAQ



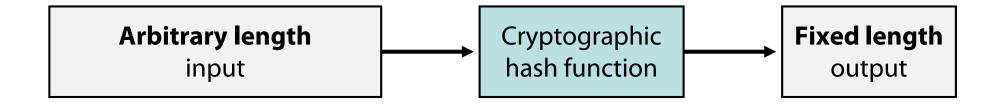
Q: What is the Commercial National Security Algorithm Suite?

A: The Commercial National Security Algorithm Suite is the suite of algorithms identified in CNSS Advisory Memorandum 02-15 for protecting NSS up to and including TOP SECRET classification. This suite of algorithms will be incorporated in a new version of the National Information Assurance Policy on the Use of Public Standards for the Secure Sharing of Information Among National Security Systems (CNSSP-15 dated October 2012). The Advisory

Algorithm	Usage		
RSA 3072-bit or larger	Key Establishment, Digital Signature		
Diffie-Hellman (DH) 3072-bit or larger	Key Establishment		
ECDH with NIST P-384	Key Establishment		
ECDSA with NIST P-384	Digital Signature		
SHA-384	Integrity		
AES-256	Confidentiality		

Cryptographic Hash Functions

Hash functions that are considered practically impossible to invert



Properties of an ideal cryptographic hash function

Easy to compute the hash value for any given message Infeasible to generate a message that has a given hash Infeasible to modify a message without changing the hash Infeasible to find two different messages with the same hash

Many-to-one function: collisions can happen

Cryptographic Hash Function Properties

Pre-image resistance

Given a hash value h, it should be computationally infeasible to find any input m such that h = hash(m)

Example: break a hashed password

Second pre-image resistance

Given an input m_1 , it should be computationally infeasible to find another input m_2 such that $m_1 \neq m_2$ and $hash(m_1) = hash(m_2)$

Example: forge an existing certificate

Collision Resistance

It should be computationally infeasible to find two different inputs m_1 and m_2 such that $hash(m_1) = hash(m_2)$ (collision)

Example: prepare two contradicting versions of a contract

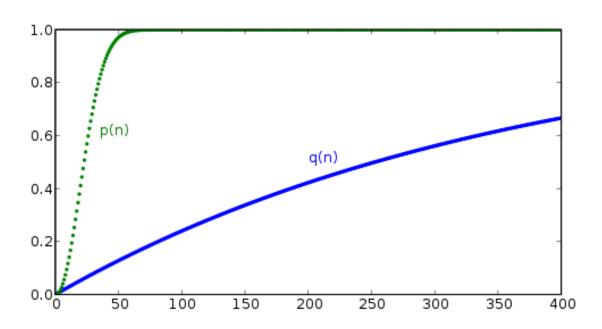
Birthday Paradox

How many people does it take before the odds are 50% or better of having

... another person with the same birthday as you? 253
Second pre-image resistance

... two people with the same birthday?

Collision resistance



Uses of Cryptographic Hash Functions

Data integrity

Digital signatures

Message authentication

User authentication

Timestamping

Certificate revocation management

Common Hash Functions

MD5: 128-bit output

1993: Boer and Bosselaers, "pseudo-collision" in which 2 different IVs produce an identical digest

1996: Dobbertin, collision of the MD5 compression function

2004: Wang, Feng, Lai, and Yu, collisions for the full MD5

2005: Lenstra, Wang, and de Weger, construction of X.509 certs with different public keys but same hash

2008: Sotirov, Stevens, Appelbaum, Lenstra, Molnar, Osvik, de Wege, creation of rogue CA certificates

Use it? NO, it's unsafe

SHA-1: 160-bit output

2005: Rijmen and Oswald, attack on a reduced version of SHA1 (53 out of 80 rounds)

2005: Wang, Yao, and Yao, lowered the complexity for finding a collision to 2⁶³

2006: Rechberger, attack with 2³⁵ compression function evaluations

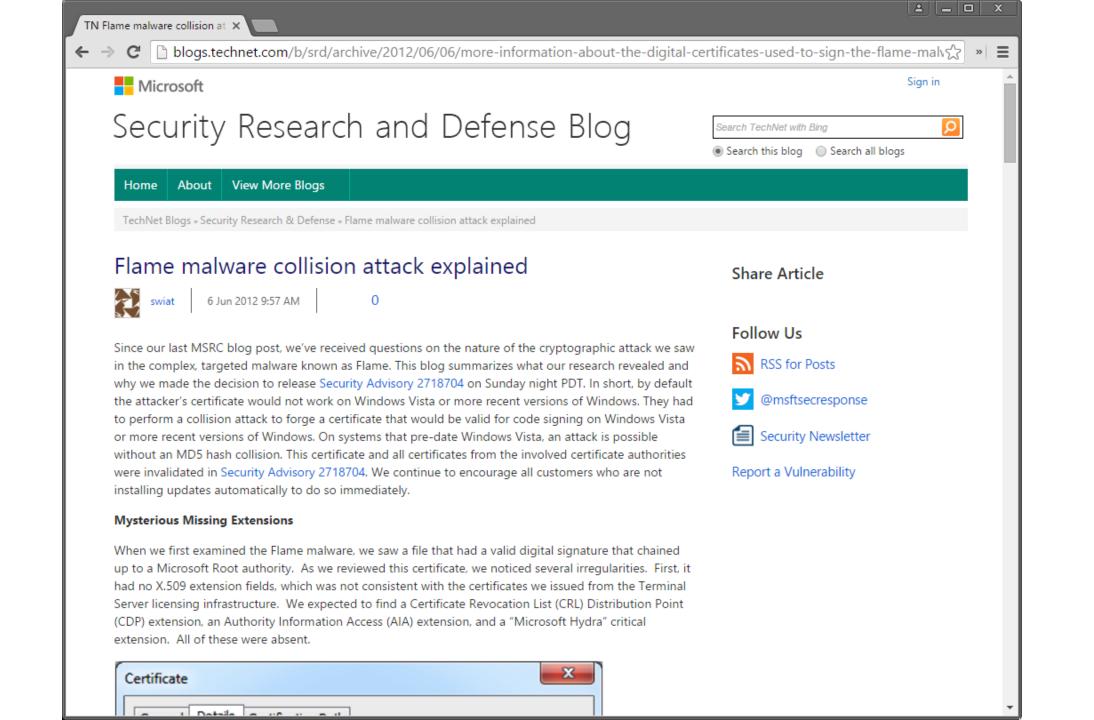
2015: Stevens, Karpman, and Thomas, freestart collision attack

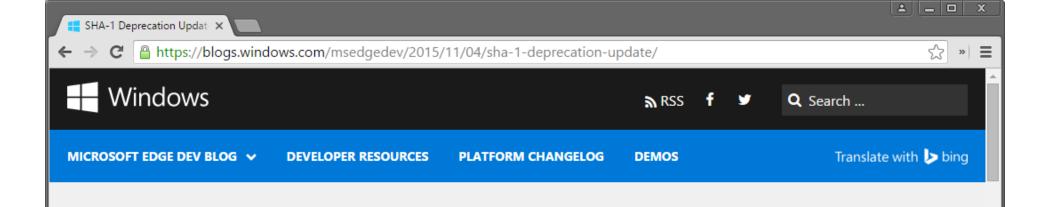
2017: SHAttered attack, generated two different PDF files with the same SHA-1 hash

2020: Leurent and Peyrin, chosen-prefix collision attack with a complexity of 2^{63,4} (~45K USD per collision)

Use it? NO, use SHA-256 or better instead







NOVEMBER 4, 2015 10:00 AM

SHA-1 Deprecation Update

By Kyle Pflug / Program Manager, Microsoft Edge

In a previous update on TechNet, we announced that Windows will block SHA-1 signed TLS certificates starting on January 1, 2017. In light of recent advances in attacks on the SHA-1 algorithm, we are now considering an accelerated timeline to deprecate SHA-1 signed TLS certificates as early as June 2016.

Mozilla recently announced a similar intent on the Mozilla Security Blog. We will continue to coordinate with other browser vendors to evaluate the impact of this timeline based on telemetry and current projections for feasibility of SHA-1 collisions.

For more details on our schedule, please see Windows Enforcement of Authenticode Code Signing and Timestamping on Technet, or

RELATED POSTS

HTTP Strict Transport Security comes to Internet Explorer 11 on Windows 8.1 and Windows 7

Read more

Ending support for the RC4 cipher in Microsoft Edge and Internet Explorer 11

Read more

How Microsoft Edge and Internet Explorer 11 on Windows 10 work better together in the Enterprise

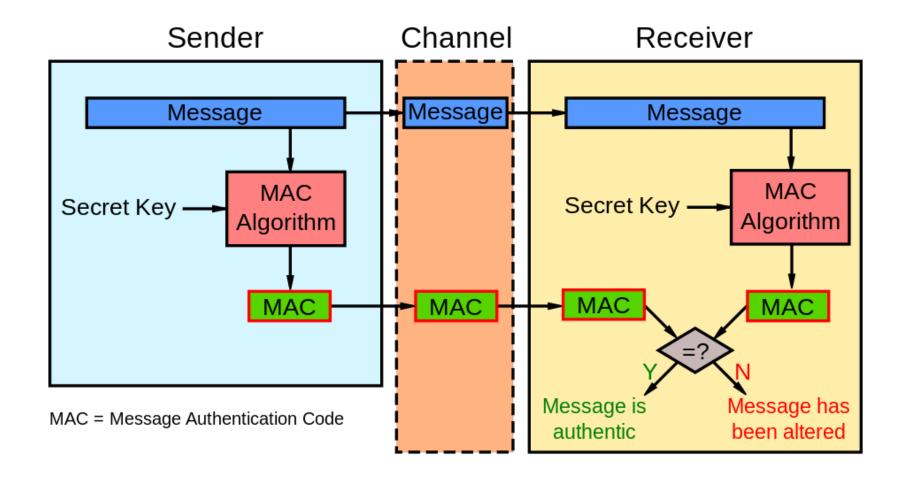
Read more

Protecting Microsoft Edge against binary injection

Read more

Message Authentication Codes (MACs)

Verify both message integrity and authenticity



$MAC = H(key \parallel message)$

denotes concatenation

Problem: easy to append data to the message without knowing the key and obtain another valid MAC

Length-extension attack: calculate $H(m_1 \parallel m_2)$ for an attacker-controlled m_2 given only $H(m_1)$ and the length of m_1

Keyed-hash message authentication code (HMAC)

$$\mathsf{HMAC}(K, m) = \mathsf{H}((K \oplus opad) || \mathsf{H}(K \oplus ipad || m))$$

opad/ipad: outer/inner padding

Impossible to generate the HMAC of a message without knowing the secret key

Double nesting prevents various forms of length-extension attacks

Order of Encryption and MACing

Encrypted data usually must be protected with a MAC

Encryption alone protects only against passive adversaries

Different options:

MAC-and-Encrypt
$$E(P) \parallel M(P)$$

No integrity of the ciphertext

MAC-then-Encrypt
$$E(P \parallel M(P))$$

No integrity of the ciphertext (have to decrypt it first)

Encrypt-then-MAC
$$E(P) \parallel M(E(P))$$

Provides integrity of the ciphertext

Preferable option – always MAC the ciphertext

Digital Signatures

Use RSA backwards:

Sign (encrypt) with the private key

Verify (decrypt) with the public key

Ownership of a private key turns it into a digital signature

Anyone can verify that a message was signed by its owner → Non-repudiation

Again, too expensive to sign the whole message

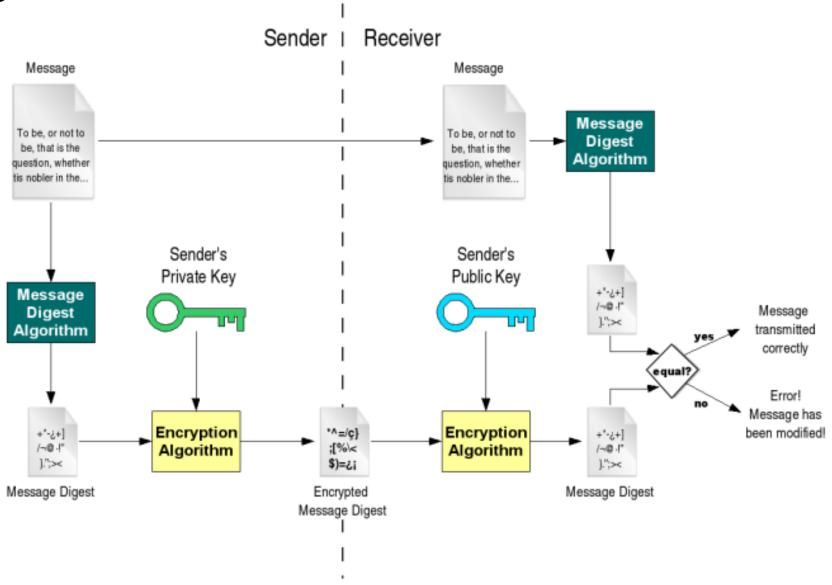
Calculate a cryptographic hash of the message and then sign the hash

What if a private key was stolen or deliberately leaked?

All signatures (past and future) of that signer become suspect

The signer might know which signatures were issued legitimately, but there is no way for the verifier to distinguish between them

Digital Signatures



Hashes vs. MACs vs. Digital Signatures

	Hash	MAC	Signature
Integrity	✓	√	✓
Authentication		\checkmark	\checkmark
Non-repudiation			\checkmark
Keys	None	Symmetric	Asymmetric

Public Key Authenticity

Authentication without confidence in the keys used is pointless

Need to obtain evidence that a given public key is authentic

It is correct and belongs to the person or entity claimed

Has not been tampered with or replaced by an attacker

Different ways to establish trust (future lecture)

TOFU: trust on first use (e.g., SSH)

Web of trust: decentralized trust model (e.g., PGP)

PKI: public key infrastructure (e.g., TLS)

Adi Shamir: Crypto is typically bypassed, not penetrated

