Programming Language Syntax

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Programming Languages Syntax

Computer languages must be precise:

- Both their form (syntax) and meaning (semantics) must be specified without ambiguity, so that both programmers and computers can tell what a program is supposed to do.
- Example: the syntax of Arabic numerals:
 - A *digit* "is": 0 |(or) 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
 - A non_zero_digit "is" 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
 - A natural_number (>0)"is"a non_zero_digit followed by other digits (a number that doesn't start with 0) = the regular expression "non_zero_digit digit*"
- Specifying the syntax for programming languages has 2 parts: Regular Expressions (RE) and Context-Free Grammars

Regular Expressions

- A *regular expression* is one of the following:
 - a character
 - \bullet the empty string, denoted by ϵ
 - two regular expressions concatenated
 - E.g., letter letter
 - two regular expressions separated by | (i.e., or),
 - E.g., letter (letter | digit)
 - a regular expression followed by the *Kleene star* (concatenation of zero or more previous item)
 - E.g., letter (letter | digit)*

Regular Expressions

- RE example: the syntax of numeric constants can be defined with regular expressions:
- 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 A digit "is" A number "is" integer | real An *integer* "is" digit digit* A real "is" integer exponent | decimal (exponent | E) A decimal "is" digit* (.digit | digit.) digit* An exponent "is" ($e \mid E$) ($+ \mid - \mid E$) integer

Regular Expressions

- Regular expressions work well for defining tokens
 - They are unable to specify nested constructs
 - For example, a context free grammar in BNF form to define arithmetical expressions is:
- $expr \rightarrow id \mid number \mid expr \mid (expr) \mid expr op expr$ $op \rightarrow + \mid - \mid * \mid /$

• Same number of open and closed parenthesis cannot be represented by RE

Chomsky Hierarchy

- Context Free Languages are strictly more powerful than Regular Expressions, BUT, Regular Expressions are way faster to recognize, so
 - Regular Expressions are used to create tokens, the leafs of the syntax tree, while Context Free grammars build the syntax tree

• Chomsky Hierarchy:

- Type-3: Regular Languages (Regex) implemented by Finite Automata (called Lexer, Scanner, Tokenizer)
- Type-2: Context-Free Languages Pushdown Automata (called Parsers)
- Type-1: Context-Sensitive Language
- Type-0: Unrestricted Language Turing Machine
- Types 0 and 1 are not for practical use in defining programming languages
- Type 2, for very restricted practical use $(O(N^3)$ in the worst case)

Type 3 are fast (linear time to recognize tokens), but not expressive enough for most languages (c) Paul Fodor (CS Stony Brook) and Elsevier

- Backus-Naur Form (BNF) notation for CFG: expr \rightarrow id | number | - expr | (expr) | expr op expr op \rightarrow + | - | * | /
 - Each of the rules in a CFG is known as a *production*
 - The symbols on the left-hand sides of the productions are *nonterminals* (or *variables*)
- A CFG consists of:
 - a set of terminals/tokens T (that <u>cannot appear on the</u> <u>left-hand side of any production</u>)
 - a set of non-terminals N
 - a non-terminal start symbol S, and
 - a set of productions

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- John Backus was the inventor of Fortran (won the ACM Turing Award in 1977)
- John Backus and Peter Naur used the BNF form for Algol
- Peter Naur also won the ACM Turing Award in 2005 for *Report on the Algorithmic Language ALGOL 60*BNF was named by Donald Knuth

 The Kleene star * and meta-level parentheses of regular expressions do not change the expressive power of the notation

• From RE to BNF notation:

• Consider the RE: a* (b a* b)*

• Start with **a***:

As -> a As

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- Same with (b a* b)*. It is:
- $S \rightarrow b As b S$

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Now you concatenate them into a single non-terminal: **G** –> **As S**

- **Derivations and Parse Trees**: A context-free grammar shows us how to **generate** a syntactically valid string of terminals
 - 1. Begin with the start symbol
 - 2. Choose a production with the <u>start symbol on the left-hand side;</u> replace the start symbol with the right-hand side of that production
 - Now choose a nonterminal A in the resulting string, choose a production P with A on its left-hand side, and replace A with the right-hand side of P
 - Repeat this process until no non-terminals remain
 - The replacement strategy named *right-most derivation* chooses at each step to replace the right-most nonterminal with the right-hand side of some production
 - There are many other possible derivations, including *left-most* and options in between.

- Example: we can use our grammar for expressions to generate the string "slope * x + intercept": Grammar: $expr \Rightarrow expr \text{ op } expr$ $expr \rightarrow id \mid number$ $\Rightarrow \exp r \operatorname{op} id$ $|-\exp|(\exp)|$ $\Rightarrow \underline{\operatorname{expr}} + \operatorname{id}$ \Rightarrow expr op <u>expr</u> + id expr op expr $\Rightarrow \exp \operatorname{op} \operatorname{id} + \operatorname{id}$ $op \rightarrow + |-| * |/$ $\Rightarrow \underline{\operatorname{expr}} * \operatorname{id} + \operatorname{id}$
 - \Rightarrow id(*slope*)* id(*x*)+ id(*intercept*)

 \Rightarrow id * id + id

Notes: The \Rightarrow metasymbol is often pronounced "*derives*"

- A series of replacement operations that shows how to derive a string of terminals from the start symbol is called a *derivation*
- Each string of symbols along the way is called a *sentential form*
- The final sentential form, consisting of only terminals, is called the *yield* of the derivation

Derivations and Parse Trees

- We can represent a derivation graphically as a *parse tree*
 - The root of the parse tree is the start symbol of the

grammar

- The leaves are its yield
- Each node with its

children represent a production

- E.g., The parse tree for the expression grammar for
 - **3 + 4 * 5** is:





Context free grammars

• A better version of our expression grammar should include precedence and associativity:

 $expr \rightarrow term \mid expr \ add_op \ term$ $term \rightarrow factor \mid term \ mult_op \ factor$ $factor \rightarrow id \mid number \mid - factor \mid (expr)$ $add_op \rightarrow + \mid mult_op \rightarrow * \mid /$



Parse tree for 3 + 4 * 5, with precedence



• has *left associativity*

 $expr \rightarrow term \mid expr \ add_op \ term$ $term \rightarrow factor \mid term \ mult_op \ factor$ $factor \rightarrow id \mid number \mid - factor \mid (\ expr \)$ $add_op \rightarrow + \mid$ $mult_op \rightarrow * \mid /$

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- The scanner and parser for a programming language are responsible for discovering the syntactic structure of a program (i.e., the *syntax analysis*)
- The *scanner/lexer* is responsible for
 - tokenizing source
 - removing comments
 - (often) dealing with pragmas (i.e., significant comments)
 - saving text of identifiers, numbers, strings
 - saving source locations (file, line, column) for error

- The Scanner turns a program into a string of tokens
- It matches <u>regular expressions</u> (usually written in Perl style regex) to a program and creates a list of tokens
 - There are two syntaxes for regular expressions: Perl-style Regex and EBNF
- Scanners tend to be built three ways:
 - Writing / Generating a finite automaton from REs
 - Scanner code (usually realized as nested if/case statements)
 - Table-driven DFA
- Writing / Generating a finite automaton generally yields the fastest, most compact code by doing lots of special-purpose things, although good automatically-generated scanners come very close

• Construction of an NFA equivalent to a given regular expression: cases





Scanning Construction of an NFA equivalent to the regular expression d* (.d | d.) d*













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- From an NFA to a DFA:
 - Reason: With no way to "guess" the right transition to take from any given state, any practical implementation of an NFA would need to explore all possible transitions concurrently or via backtracking
 - We can instead build a DFA from that NFA:
 - The state of the DFA after reading any input will be the set of states that the NFA might have reached on the same input
 - Our example: Initially, before it consumes any input, the NFA may be in **State 1**, or it may make <u>epsilon transitions</u> to **States 2, 4, 5, or 8**

• We thus create an initial **State A** for our DFA to represent this set: **1,2,4,5,8**

- On an input of d, our NFA may move from State 2 to State 3, or from State 8 to State 9.
 - It has no other transitions on this input from any of the states in A.
 - From **State 3**, however, the NFA may make epsilon transitions to any of **States 2, 4, 5, or 8**.
 - We therefore create DFA **State B: 2, 3, 4, 5, 8, 9**
- On a ., our NFA may move from **State 5** to **State 6**
 - There are no other transitions on this input from any of the states in A, and there are no epsilon transitions out of **State 6**.
 - We therefore create the singleton DFA **State C:6**
- We continue the process until we find all the states and transitions in the DFA (it is a finite process Why?)



Scanner code (usually realized as nested if/case statements)

- Suppose we are building an *ad-hoc (hand-written) scanner* for a Calculator:
 - assign \rightarrow := plus \rightarrow + minus \rightarrow times \rightarrow * div \rightarrow / lparen \rightarrow (rparen \rightarrow) id \rightarrow letter (letter | digit)* number \rightarrow digit digit * | digit * (. digit | digit .) digit *

• We read the characters one at a time with look-ahead

skip any initial white space (spaces, tabs, and newlines)

if cur_char $\in \{ (', ')', '+', '-', '*' \}$

return the corresponding single-character token if cur char = `:'

read the next character

if it is '=' then return *assign* else announce an error if cur char = '/'

peek at the next character

if it is '*' or '/'

read additional characters until "*/" or newline

is seen, respectively

jump back to top of code

else return div

if cur char = .read the next character if it is a digit read any additional digits return number else announce an error if cur char is a digit read any additional digits and at most one decimal point return number if cur char is a letter read any additional letters and digits check to see whether the resulting string is read or write if so then return the corresponding token else return id

else announce an error

Scanning Pictorial Start 1 representation of a scanner for calculator tokens, in the form of a finite automaton digit



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- We run the machine over and over to get one token after another
 - •Nearly universal rule:
 - always take the longest possible token from the input thus foobar is foobar and never f or foo or foob
 - more to the point, 3.14159 is a real constant and never 3, ., and 14159

Integer")

- The rule about longest-possible tokens means you return only when the next character can't be used to continue the current token
 - the next character will generally need to be saved for the next token
- In some cases, you may need to peek at more than one character of look-ahead in order to know whether to proceed
 - In Pascal, for example, when you have a **3** and you a see a dot
 - do you proceed (in hopes of getting **3.14**)? or
 - do you stop (in fear of getting 3..5)? (declaration of arrays in Pascal, e.g., "array [1..6] of

Scanning • Writing a pure DFA as a set of nested case statements is a surprisingly useful programming technique •use perl, awk, sed • Table-driven DFA is what **lex** and scangen produce •lex (flex) in the form of C code •**scangen** in the form of numeric tables and a separate driver 32 (c) Paul Fodor (CS Stony Brook) and Elsevier

Perl-style Regexp

• Learning by examples: abcd - concatenation a (b|c)d - grouping **a** (**b** | **c**) ***d** - can apply a number of repeats to char or group ? = 0 - 1***** = 0-inf **+** = 1-inf **[bc]** - character class **[a-zA-Z0-9**] - ranges • - matches any character. **\a** - alpha **\d** - numeric \mathbf{W} - word (alpha, num, _) **\s** - whitespace

Perl-style Regexp

 Learning by examples: How do we write a regexp that matches floats?

digit*(.digit|digit.)digit*

\d*(\.\d|\d \.)\d*

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Parsing

- The *parser* calls the scanner to get the tokens, assembles the tokens together into a *syntax tree*, and passes the tree (perhaps one subroutine at a time) to the later phases of the compiler (this process is called *syntax-directed translation*).
- Most use a context-free grammar (CFG)

Parsing

• It turns out that for any CFG we can create a parser that runs in $O(n^3)$ time (e.g., Earley's algorithm and the Cocke-Younger-Kasami (CYK) algorithm) •O (n³) time is clearly unacceptable for a parser in a compiler - too slow even for a program of 100 tokens (~1,000,000 cycles)
- Parsing
 Fortunately, there are large classes of grammars for which we can build parsers that run in linear time
 - The two most important classes are called LL and LR
 - LL stands for Left-to-right, Leftmost derivation
 - Leftmost derivation work on the left side of the parse tree
 - LR stands for Left-to-right, Rightmost derivation
 - Rightmost derivation work on the right side of the tree
 - LL parsers are also called '*top-down*', or '*predictive*' parsers
 - LR parsers are also called 'bottom-up', or 'shift-reduce' parsers

Top-down parsing (LL)

Consider a grammar for a comma separated list of identifiers, terminated by a semicolon:

id_list → **id** *id_list_tail id_list_tail* → , **id** *id_list_tail id_list_tail* → ;

The top-down construction of a parse tree for the string: "A, B, C;" starts from the root and applies rules and tried to identify nodes.



Bottom-up parsing (LR)

id_list → **id** *id_list_tail id_list_tail* → , **id** *id_list_tail id_list_tail* → ;

- The bottom-up construction of a parse tree for the same string:
 "A, B, C;"
- The parser finds the left-most leaf of the tree is an id. The next leaf is a comma. The parser continues in this fashion, shifting new leaves from the scanner into a forest of partially completed parse tree fragments.



Bottom-up parsing (LR)

- The bottom-up construction realizes that **some of those fragments constitute a complete right-hand side.**
- In this grammar, that occur when the parser has seen the semicolon the right-hand side of *id_list_tail*.
 With this right-hand side in hand, the parser **reduces** the semicolon to an *id_list_tail*.
- It then **reduces** ", **id** *id_list_tail*" into another *id_list_tail*.
- After doing this one more time it is able to reduce "id *id_list_tail*" into the root of the parse tree, *id_list*.



Parsing

- The number in LL(1), LL(2), ..., indicates how many tokens of look-ahead are required in order to parse
 - Almost all real compilers use **one token** of lookahead
- LL grammars requirements:
 no left recursion
 - no common prefixes
- Every LL(1) grammar is also LR(1), though right recursion in production tends to require very deep stacks and complicates semantic analysis

An LL(1) grammar

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```
program \rightarrow stmt list $$(end of file)
stmt list \rightarrow stmt stmt list
                   ε
stmt \rightarrow id := expr
                | read id
                | write expr
expr \rightarrow term term tail
term tail \rightarrow add op term term tail
                Ιε
term \rightarrow factor fact tailt
fact tail \rightarrow mult op factor fact tail
                3
factor
                \rightarrow ( expr )
                | id
                | number
 add op
                \rightarrow +
 mult op
                   *
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```

- This grammar captures associativity and precedence, but most people don't find it as pretty
 - for one thing, the operands of a given operator aren't in a Right Hand Side (RHS) together!
 - however, the simplicity of the parsing algorithm makes up for this weakness
 - The first parsers were LL
- How do we parse a string with this grammar?by building the parse tree incrementally

LL Parsing • Example (the average program): read A read B sum := A + Bwrite sum write sum / 2 \$\$

- We keep a stack of non-terminals with the start symbol inserted
- We start at the top and predict needed productions on the basis of the <u>current "left-most" non-terminal</u> in the tree and the <u>current input token</u>

- Table-driven LL parsing: you have a big loop in which you repeatedly look up an action in a two-dimensional table based on current leftmost non-terminal and current input token
- The actions are:
 - (1) match a terminal
 - (2) predict a production OR
 - (3) announce a syntax error

 First, unfold the production rules to collect for each production the possible tokens that could start it

PREDICT

 program → stmt_list \$\$ {id, read, write, \$\$} stmt_list → stmt stmt_list {id, read, write} 3. stmt_list $\longrightarrow \in \{\$\$\}$ 4. stmt \rightarrow id := expr {id} 5. stmt \longrightarrow read id {read} 6. stmt → write expr {write} 7. $expr \longrightarrow term term_tail \{(, id, number\}\}$ 8. term_tail \longrightarrow add_op term term_tail {+, -} 9. $term_tail \longrightarrow \epsilon$ {), id, read, write, \$\$} 10. term \longrightarrow factor factor_tail { (, id, number } 11. factor_tail \longrightarrow mult_op factor factor_tail {*, /} 12. factor_tail $\longrightarrow \in \{+, -, \}, id, read, write, \$\}$ 13. factor \rightarrow (expr) {(} 14. factor \rightarrow id {id} 15. factor \rightarrow number {number} 16. $add_op \longrightarrow + \{+\}$ 17. $add_{op} \rightarrow - \{-\}$ 18. $mult_op \longrightarrow * \{*\}$ 19. $mult_op \rightarrow / \{/\}$

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• Construct the *prediction table*: for each possible input token and the left-most nonterminal, what is the possible production rule that will be used?

• The non-terminal will be "used", while the RHS of the production is added to the stack.

PREDICT

- program → stmt_list \$\$ {id, read, write, \$\$}
- stmt_list → stmt stmt_list {id, read, write}
- 3. $stmt_list \longrightarrow \epsilon \{\$\$\}$
- 4. $stmt \longrightarrow id := expr\{id\}$
- 5. $stmt \longrightarrow read id \{read\}$
- 6. $stmt \longrightarrow write expr \{write\}$
- 7. $expr \longrightarrow term term_tail \{(, id, number\}\}$
- 8. term_tail \rightarrow add_op term term_tail {+, -}
- 9. $term_tail \longrightarrow \epsilon$ {), id, read, write, \$\$}
- 10. term \longrightarrow factor factor_tail { (, id, number }
- 11. factor_tail \longrightarrow mult_op factor factor_tail {*, /} 12. factor_tail $\longrightarrow \epsilon$ {+, -,), id, read, write, \$\$
- 13. factor \rightarrow (expr) {(}
- 14. factor \longrightarrow id {id}
- 15. factor \longrightarrow number {number}
- 16. $add_op \longrightarrow + \{+\}$
- 17. $add_op \longrightarrow \{-\}$ 18. $mult_op \longrightarrow * \{*\}$
- 19. $mult_op \longrightarrow / \{/\}$

Top-of-stack		Current input token										
nonterminal	id	number	read	write	:=	()	+	-	*	/	\$\$
program	1	-	1	1			—					1
$stmt_list$	2	4 0	2	2	133	5		1		<u>a</u> _8		3
stmt	4	-	5	6							-	(1
expr	$\overline{7}$	7		<u>(2)</u>	22 <u></u> 2	$\overline{7}$	(<u>*</u>))	(2 <u></u>)		1 <u></u>	<u>(*</u> 1)	
$term_tail$	9		9	9	-	—	9	8	8		—	9
term	10	10		<u> 20 -</u>		10	<u> </u>		<u> </u>	<u>. </u>		23 <u></u> 2
$factor_tail$	12	-	12	12		—	12	12	12	11	11	12
factor	14	15		<u>121</u>		13	0	2 <u></u> 2	<u> </u>			64 <u>—14</u>
add_op		-			-		-	16	17		-	_
$mult_op$			<u>19</u>	<u>10</u>	s <u></u> s	<u>-</u>	<u></u>	2 <u></u>		18	19	17 <u></u>

LL Parsing
 LL(1) parse table for parsing for
calculator language
read A
read B
sum := A + B
write sum
write sum / 2 \$\$

PREDICT program → stmt_list \$\$ {id, read, write, \$\$} stmt_list → stmt stmt_list {id, read, write} 3. stmt_list $\longrightarrow \in \{\$\}$ 4. stmt \rightarrow id := expr {id} 5. stmt \longrightarrow read id {read} 6. stmt \longrightarrow write expr {write} 7. $expr \longrightarrow term term_tail \{(, id, number\}\}$ 8. term_tail \longrightarrow add_op term term_tail {+, -} 9. $term_tail \longrightarrow \epsilon$ {), id, read, write, \$\$} 10. term \longrightarrow factor factor_tail { (, id, number } 11. factor_tail \longrightarrow mult_op factor factor_tail {*, /} 12. factor_tail $\longrightarrow \epsilon \{+, -, \}, id, read, write, \$\}$ 13. factor \rightarrow (expr) { (} 14. factor \rightarrow id {id} 15. factor \longrightarrow number {number} 16. $add_op \longrightarrow + \{+\}$ 17. $add_op \longrightarrow - \{-\}$ 18. $mult_op \longrightarrow * \{*\}$ 19. $mult_op \longrightarrow / \{/\}$

Top-of-stack Current input token													
$\operatorname{nonterminal}$	id	number	read	write	:=	()	+	-	*	/	\$\$	
program	1	-	1	1		-	—					1	
$stmt_list$	2	8 0	2	2	10	5		10		a_3		3	
stmt	4	-	5	6	—	-		-			-		
expr	$\overline{7}$	7		<u>(2)</u>	(2 <u></u>)	$\overline{7}$	(<u>*</u>))	(2 <u></u>)		<u>12</u> 11	<u></u>	23 <u>13</u>	
$term_tail$	9		9	9	—	—	9	8	8		-	9	
term	10	10		<u> 20 -</u>		10	<u> </u>	2 <u></u> 2	<u> </u>		- <u>-</u>	93 <u></u> 2	
$factor_tail$	12	-	12	12	-	—	12	12	12	11	11	12	
factor	14	15		<u>101</u>		13	0		<u> </u>	<u>1000</u> 1		N=	
add_op		-	_		-	-	-	16	17		-		
mult_op		1 <u></u>		<u> 2</u>	1 <u></u> 2		-	5 <u></u>		18	19	11 <u></u>	

	Parse stack	Input stream	Comment
	program	read A read B	
	stmt_list \$\$	read A read B	predict program \longrightarrow stmt_list \$\$
	stmt stmt_list \$\$	read A read B	predict $stmt_list \longrightarrow stmt \ stmt_list$
	<pre>read id stmt_list \$\$</pre>	read A read B	predict $stmt \longrightarrow read$ id
	id stmt_list \$\$	A read B	match read
	stmt_list \$\$	read B sum :=	match id
	stmt stmt_list \$\$	read B sum :=	predict $stmt_list \longrightarrow stmt \ stmt_list$
	<pre>read id stmt_list \$\$</pre>	read B sum :=	predict $stmt \longrightarrow read$ id
	id stmt_list \$\$	B sum :=	match read
	stmt_list \$\$	sum := A + B	match id
	stmt stmt_list \$\$	sum := A + B	predict <i>stmt_list</i> \longrightarrow <i>stmt stmt_list</i>
	<pre>id := expr stmt_list \$\$</pre>	sum := A + B	predict $stmt \longrightarrow id := expr$
	:= expr stmt_list \$\$:= A + B	match id
	expr stmt_list \$\$	A + B	match :=
	term term_tail stmt_list \$\$	A + B	predict $expr \longrightarrow term \ term_tail$
	factor factor_tail term_tail stmt_list \$\$	A + B	predict term \longrightarrow factor factor_tail
	<pre>id factor_tail term_tail stmt_list \$\$</pre>	A + B	predict <i>factor</i> \longrightarrow id
	factor_tail term_tail stmt_list \$\$	+ B write sum	match id
	term_tail stmt_list \$\$	+ B write sum	predict factor_tail $\longrightarrow \epsilon$
	add_op term term_tail stmt_list \$\$	+ B write sum	predict $term_tail \longrightarrow add_op term term_tail$
	+ term term_tail stmt_list \$\$	+ B write sum	predict $add_op \longrightarrow +$
	term term_tail stmt_list \$\$	B write sum	match +
	factor factor_tail term_tail stmt_list \$\$	B write sum	predict <i>term</i> \longrightarrow <i>factor factor_tail</i>
	id factor_tail term_tail stmt_list \$\$	B write sum	predict <i>factor</i> \longrightarrow id
	factor_tail term_tail stmt_list \$\$	write sum	match id
	term_tail stmt_list \$\$	write sum write	predict factor_tail $\longrightarrow \epsilon$
	stmt_list \$\$	write sum write	predict $term_tail \longrightarrow \epsilon$
	stmt stmt_list \$\$	write sum write	predict $stmt_list \longrightarrow stmt \ stmt_list$
<	<pre>write expr stmt_list \$\$</pre>	write sum write	predict stmt \longrightarrow write expr

expr stmt_list \$\$ term term_tail stmt_list \$\$ factor factor_tail term_tail stmt_list \$\$ id factor_tail term_tail stmt_list \$\$ factor_tail term_tail stmt_list \$\$ term_tail stmt_list \$\$ stmt_list \$\$ stmt stmt_list \$\$ write expr stmt_list \$\$ expr stmt_list \$\$ term term_tail stmt_list **\$\$** factor factor_tail term_tail stmt_list \$\$ id factor_tail term_tail stmt_list \$\$ factor_tail term_tail stmt_list \$\$ mult_op factor factor_tail term_tail stmt_list \$\$ / factor factor_tail term_tail stmt_list \$\$ factor factor_tail term_tail stmt_list \$\$ number factor_tail term_tail stmt_list \$\$ factor_tail term_tail stmt_list \$\$ term_tail stmt_list \$\$ stmt_list \$\$ \$\$

sum write sum / 2 write sum / 2 write sum /2write sum / 2 write sum / 2 write sum /2sum / 2 sum / 2sum / 2sum / 212 12 12 2 2

match write predict expr \longrightarrow term term_tail predict term \longrightarrow factor factor_tail predict *factor* \longrightarrow **id** match id predict factor_tail $\longrightarrow \epsilon$ predict term_tail $\longrightarrow \epsilon$ predict stmt_list \longrightarrow stmt stmt_list predict stmt \longrightarrow write expr match write predict $expr \longrightarrow term term_tail$ predict term \longrightarrow factor factor_tail predict *factor* \longrightarrow **id** match id predict factor_tail \longrightarrow mult_op factor factor_tail predict $mult_op \longrightarrow /$ match / predict *factor* \rightarrow **number** match number predict factor_tail $\longrightarrow \epsilon$ predict term_tail $\longrightarrow \epsilon$ predict stmt_list $\longrightarrow \epsilon$



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- Problems trying to make a grammar LL(1)
 left recursion
 - example:

 - we can get rid of all left recursion mechanically in any grammar

- Problems trying to make a grammar LL(1)
 common prefixes
 - example:
 - stmt \rightarrow id := expr
 - | id (arg_list)
 we can eliminate left-factor mechanically =
 "left-factoring"
 stmt → id id_stmt_tail
 id stmt tail → := expr
 - $\frac{\text{sumt_tarr}}{| (\text{arg_list})|}$

- Eliminating left recursion and common prefixes still does NOT make a grammar LL
 - there are infinitely many non-LL LANGUAGES, and the mechanical transformations work on them just fine
- Problems trying to make a grammar LL(1)
 - the "dangling else" problem prevents grammars from being LL(1) (or in fact LL(k) for any k)
 - the following natural (Pascal) grammar fragment is ambiguous:

stmt -> if cond then_clause else_clause
 | other stuff

then_clause \rightarrow then stmt

else_clause → else stmt | ε Example String: "if C1 then if C2 then S1 else S2"

Ambiguity: the else can be paired with either if then!!!

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- Desired effect: pair the else with the nearest then.
- The less natural grammar fragment:
 stmt → balanced_stmt | unbalanced_stmt
 balanced_stmt → if cond then balanced_stmt
 else balanced_stmt
 | other_stuff
 unbalanced_stmt → if cond then stmt
 | if cond then balanced_stmt
 else unbalanced stmt
- A **balanced_stmt** is one with the same number of **thens** and **elses**.
- An **unbalanced_stmt** has more **then**s.

• The <u>usual</u> approach, whether top-down OR bottom-up, is to <u>use the ambiguous grammar</u> together with a disambiguating rule that says: • <u>else goes with the closest then</u> or •more generally, the first of two possible productions is the one to predict (or reduce) stmt \rightarrow if cond then clause else clause | other stuff then clause \rightarrow then stmt else clause \rightarrow else stmt | ϵ

- Better yet, languages (since Pascal) generally employ explicit end-markers, which eliminate this problem.
- In Modula-2, for example, one says:

```
if A = B then
    if C = D then E := F end
else
    G := H
end
```

• Ada says 'end if'; other languages say 'fi'

• One problem with end markers is that they tend to bunch up. In Pascal you say

if A = B then ...
else if A = C then ...
else if A = D then ...
else if A = E then ...
else ...;

• With end markers this becomes

if A = B then ...
else if A = C then ...
else if A = D then ...
else if A = E then ...
else ...;
end; end; end; end; end; end; ...

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- LR parsers are almost always **table-driven**:
 - like a table-driven LL parser, an LR parser uses a
 big loop in which it repeatedly inspects a twodimensional table to find out what action to take
 - unlike the LL parser, however, the LR driver has non-trivial state (like a DFA), and the table is indexed by current input token and current state
 - also the stack contains a record of what has been seen SO FAR (NOT what is expected)

- LR keeps the **roots of its partially completed subtrees** on a stack
 - When it accepts a new token from the scanner, it *shifts* the token into the stack
 - When it recognizes that the top few symbols on the stack constitute a right-hand side, it *reduces* those symbols to their left-hand side by popping them off the stack and pushing the left-hand side in their place

LR Parsing Rightmost (canonical) 	$id_list \rightarrow id id_list_tail$ $id_list_tail \rightarrow , id id_list_tail$ $id_list_tail \rightarrow ;$ derivation for the
identifiers grammar:	
Stack contents (roots of partial	trees) Remaining input
<pre></pre>	A, B, C; , B, C; B, C; , C; C; ;

LR(1) grammar for the calculator language:

- 1. program \rightarrow stmt_list \$\$
- 2. $stmt_list \rightarrow stmt_list stmt$
- 3. $stmt_list \rightarrow stmt$
- 4. stmt \rightarrow id := expr
- 5. stmt \rightarrow read id
- 6. stmt \rightarrow write expr
- 7. expr \rightarrow term
- 8. $expr \rightarrow expr add_op term$
- 9. term \rightarrow factor
- 10. term \rightarrow term mult_op factor
- 11. factor \rightarrow (expr)
- 12. factor \rightarrow id
- 13. factor \rightarrow number
- 14. $add_op \rightarrow +$
- 15. $add_op \rightarrow -$
- 16. $mult_op \rightarrow *$
- 17. mult_op \rightarrow /

 Example (the average program): read A read B sum := A + B write sum write sum

 When we begin execution, the parse stack is empty and we are at the beginning of the production for program:

program \rightarrow . stmt_list \$\$

- When augmented with a •, a production is called an *LR item*
- This original item (program → . stmt_list \$\$) is called the *basis* of the list.

• Since the . in this item is immediately in front of a nonterminal—namely **stmt** list —we may be about to see the yield of that nonterminal coming up on the input. program \rightarrow . stmt list \$\$ stmt list \rightarrow . stmt list stmt stmt list \rightarrow . stmt

- Since **stmt** is a nonterminal, we may also be at the beginning of any production whose left-hand side is **stmt**:
 - program → . stmt_list \$\$
 stmt_list → . stmt_list stmt
 stmt_list → . stmt
 stmt → . id := expr
 stmt → . read id
 stmt → . write expr

• The additional items to the basis are its *closure*.

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- Our upcoming token is a **read**
 - Once we shift it onto the stack, we know we are in the following state:

stmt \rightarrow read . id

- This state has a single basis item and an empty closure—the . precedes a terminal.
- After shifting the A, we have:
 stmt → read id .

- We now know that **read id** is the handle, and we must reduce.
 - The reduction pops two symbols off the parse stack and pushes a stmt in their place
 - Since one of the items in State 0 was
 - <code>stmt_list</code> \rightarrow . <code>stmt</code>

we now have

stmt_list \rightarrow stmt .

Again we must reduce: remove the **stmt** from the stack and push a **stmt list** in its place.

• Our new state:

program → stmt_list . \$\$
stmt_list → stmt_list . stmt
stmt → . id := expr
stmt → . read id
stmt → . write expr

	State	Transitions
0.	program $\longrightarrow \bullet stmt_list $	on <i>stmt_list</i> shift and goto 2
	$stmt_list \longrightarrow \bullet stmt_list stmt$ $stmt_list \longrightarrow \bullet stmt$ $stmt \longrightarrow \bullet id := expr$ $stmt \longrightarrow \bullet read id$ $stmt \longrightarrow \bullet write expr$	on <i>stmt</i> shift and reduce (pop 1 state, push <i>stmt_list</i> on input) on id shift and goto 3 on read shift and goto 1 on write shift and goto 4
1.	$\textit{stmt} \longrightarrow \texttt{read} \bullet \texttt{id}$	on id shift and reduce (pop 2 states, push stmt on input)
2.	$\begin{array}{rcl} program & \longrightarrow stmt_list & \$\$\\ stmt_list & \longrightarrow stmt_list & stmt \end{array}$	on \$\$ shift and reduce (pop 2 states, push <i>program</i> on input) on <i>stmt</i> shift and reduce (pop 2 states, push <i>stmt_list</i> on input)
	$stmt \longrightarrow \bullet$ id := $expr$ $stmt \longrightarrow \bullet$ read id $stmt \longrightarrow \bullet$ write $expr$	on id shift and goto 3 on read shift and goto 1 on write shift and goto 4
3.	$stmt \longrightarrow id \bullet := expr$	on := shift and goto 5
1 .	$stmt \longrightarrow write \bullet expr$	on <i>expr</i> shift and goto 6
	$expr \longrightarrow \bullet term$	on <i>term</i> shift and goto 7
	term $\longrightarrow \bullet$ factor term $\longrightarrow \bullet$ term mult op factor	on <i>factor</i> shift and reduce (pop 1 state, push <i>term</i> on input)
	factor $\longrightarrow \bullet$ (expr) factor $\longrightarrow \bullet$ id factor $\longrightarrow \bullet$ number	on (shift and goto 8 on id shift and reduce (pop 1 state, push <i>factor</i> on input) on number shift and reduce (pop 1 state, push <i>factor</i> on input)

5. $stmt \longrightarrow id := \bullet expr$

 $expr \longrightarrow \bullet term$ $expr \longrightarrow \bullet expr add_op term$ $term \longrightarrow \bullet factor$ $term \longrightarrow \bullet term mult_op factor$ $factor \longrightarrow \bullet (expr)$ $factor \longrightarrow \bullet id$ $factor \longrightarrow \bullet number$

6. $stmt \longrightarrow write expr \bullet$ $expr \longrightarrow expr \bullet add_op term$

> $add_op \longrightarrow \bullet +$ $add_op \longrightarrow \bullet -$

7. $expr \longrightarrow term \bullet$ $term \longrightarrow term \bullet mult_op factor$

 $mult_op \longrightarrow \bullet *$ $mult_op \longrightarrow \bullet /$

on expr shift and goto 9

on term shift and goto 7

on *factor* shift and reduce (pop 1 state, push *term* on input)

on (shift and goto 8 on id shift and reduce (pop 1 state, push *factor* on input) on number shift and reduce (pop 1 state, push *factor* on input)

on FOLLOW(stmt) = {id, read, write, \$\$} reduce
 (pop 2 states, push stmt on input)
on add_op shift and goto 10
on + shift and reduce (pop 1 state, push add_op on input)
on - shift and reduce (pop 1 state, push add_op on input)

on FOLLOW(expr) = {id, read, write, \$\$,), +, -} reduce
 (pop 1 state, push expr on input)
on wwilt at shift and gate 11

on *mult_op* shift and goto 11

on * shift and reduce (pop 1 state, push mult_op on input)
on / shift and reduce (pop 1 state, push mult_op on input)

- 8. factor \longrightarrow (expr)
 - $expr \longrightarrow \bullet term$ $expr \longrightarrow \bullet expr add_op term$ $term \longrightarrow \bullet factor$ $term \longrightarrow \bullet term mult_op factor$ $factor \longrightarrow \bullet (expr)$ $factor \longrightarrow \bullet id$ $factor \longrightarrow \bullet number$
- 9. $stmt \longrightarrow id := expr \bullet$ $expr \longrightarrow expr \bullet add_op term$

 $add_op \longrightarrow \bullet + add_op \longrightarrow \bullet -$

10. $expr \longrightarrow expr \ add_op \ \bullet \ term$

 $term \longrightarrow \bullet factor$ $term \longrightarrow \bullet term \ mult_op \ factor$ $factor \longrightarrow \bullet (\ expr)$ $factor \longrightarrow \bullet \text{ id}$ $factor \longrightarrow \bullet \text{ number}$

on expr shift and goto 12

on term shift and goto 7

on factor shift and reduce (pop 1 state, push term on input)

on (shift and goto 8 on id shift and reduce (pop 1 state, push *factor* on input) on number shift and reduce (pop 1 state, push *factor* on input)

on FOLLOW(stmt) = {id, read, write, \$\$} reduce
 (pop 3 states, push stmt on input)
on add_op shift and goto 10
on + shift and reduce (pop 1 state, push add_op on input)
on - shift and reduce (pop 1 state, push add_op on input)

on term shift and goto 13

on factor shift and reduce (pop 1 state, push term on input)

on (shift and goto 8 on id shift and reduce (pop 1 state, push *factor* on input) on number shift and reduce (pop 1 state, push *factor* on input)
11. term \longrightarrow term mult_op • factor

 $\begin{array}{l} \textit{factor} \longrightarrow \bullet (\textit{expr}) \\ \textit{factor} \longrightarrow \bullet \textit{id} \\ \textit{factor} \longrightarrow \bullet \textit{number} \end{array}$

- 12. $factor \longrightarrow (expr \bullet)$ $expr \longrightarrow expr \bullet add_op term$ $add_op \longrightarrow \bullet +$ $add_op \longrightarrow \bullet -$
- 13. $expr \longrightarrow expr \ add_op \ term \bullet$ $term \longrightarrow term \bullet mult_op \ factor$

 $\begin{array}{ccc} mult_op & \longrightarrow \bullet & \ast \\ mult_op & \longrightarrow \bullet & / \end{array}$

on *factor* shift and reduce (pop 3 states, push *term* on input)

on (shift and goto 8 on id shift and reduce (pop 1 state, push *factor* on input) on number shift and reduce (pop 1 state, push *factor* on input)

on) shift and reduce (pop 3 states, push *factor* on input) on *add_op* shift and goto 10

on + shift and reduce (pop 1 state, push add_op on input)
on - shift and reduce (pop 1 state, push add_op on input)

on FOLLOW(expr) = {id, read, write, \$\$,), +, -} reduce
 (pop 3 states, push expr on input)
on mult_op shift and goto 11
on * shift and reduce (pop 1 state, push mult_op on input)

on / shift and reduce (pop 1 state, push *mult_op* on input)

Top-of-st	ack	Current input symbol																	
state	sl	\$	е	t	f	ао	то	id	lit	r	W	:=	()	+	-	*	/	\$\$
0	s2	b3	_	-	-	_	-	s3	-	s 1	s4	_	_	_	_	_	-	_	-
1	_	_	_	_	_	_	_	b5	-	_	_	_	_	_	_	_	_	-	_
2	_	b2	_	_	-	_	_	s3	-	s 1	s4	_	_	_	-	_	-	-	b1
3	_	_	_	_	_	_	_	_	_	_	_	s5	_	_	_	_	_	_	_
4	_	_	s6	s7	b9	_	_	b12	b13	_	_	_	s 8	_	_	_	_	_	_
5	_	_	s9	s7	b9	_	_	b12	b13	_	_	_	s 8	_	_	_	_	_	_
6	_	_	_	_	_	s10	_	r6	_	r6	r6	_	_	_	b14	b15	_	_	r6
7	_	_	_	_	_	_	s11	r7	_	r7	r7	_	_	r7	r7	r7	b16	b17	r7
8	_	_	s12	s 7	b9	_	_	b12	b13	_	_	_	s 8	_	_	_	_	_	_
9	_	_	_	_	-	s10	_	r4	-	r4	r4	_	_	_	b14	b15	-	-	r4
10	_	_	_	s13	b9	_	_	b12	b13	_	_	_	s 8	_	_	_	_	_	_
11	_	_	_	_	b10	_	_	b12	b13	_	_	_	s 8	_	_	_	_	_	_
12	_	_	_	_	_	s10	_	_	_	_	_	_	_	b11	b14	b15	_	_	_
13	_	_	_	_	_	_	s11	r8	_	r8	r8	_	_	r8	r8	r8	b16	b17	r8

Table entries indicate whether to shift (s), reduce (r), or shift and then reduce (b). The accompanying number is the new state when shifting, or the production that has been recognized when (shifting and) reducing

Driver for a table-driven LR(1) parser

```
parse_stack.push((null, start_state))
cur_sym : symbol := scan
                                            -- get new token from scanner
loop
    cur_state : state := parse_stack.top.st -- peek at state at top of stack
    if cur_state = start_state and cur_sym = start_symbol
        return
                                            – – success!
    ar : action_rec := parse_tab[cur_state, cur_sym]
    case anaction
        shift:
             parse_stack.push((cur_sym, ar.new_state))
                                            -- get new token from scanner
             cur_sym := scan
        reduce:
             cur_sym := prod_tab[ar.prod].lhs
             parse_stack.pop(prod_tab[ar.prod].rhs_len)
        shift_reduce:
             cur_sym := prod_tab[ar.prod].lhs
             parse_stack.pop(prod_tab[ar.prod].rhs_len-1)
         error:
             parse_error
```



Parsing summary

- A <u>scanner</u> is a DFA
 - it can be specified with a state diagram
- An LL or LR **<u>parser</u>** is a PDA (push down automata)
 - a PDA can be specified with a *state diagram* and a stack
 - the state diagram looks just like a DFA state diagram, except the arcs are labeled with **<input** symbol, top-of-stack symbol> pairs, and in addition to moving to a new state the PDA has the option of pushing or popping a finite number of symbols onto/off the stack • Early's algorithm does NOT use PDAs, but dynamic programming

Actions

- We can run actions when a rule triggers:
 Often used to construct an AST for a compiler.
 - •For simple languages, can interpret code directly
 - •We can use actions to fix the Top-Down Parsing problems

Programming

- A *compiler-compiler* (or *parser generator*, *compiler generator*) is a programming tool that creates a parser, interpreter, or compiler from some form of formal description of a language and machine
 - the input is a grammar (usually in BNF) of a programming language
 - the generated output is the source code of a parser
- Examples of parser generators:
 - classical parsing tools: lex, Yacc, bison, flex, ANTLR
 - **PLY**: python implementation of **lex** and **yacc**
 - Python **TPG** parser
 - **ANTLR** for python

Classic Parsing Tools

lex - original UNIX Lexical analysis (tokenizing) generator

• create a C function that will parse input according to a set of regular expressions

yacc - Yet Another Compiler Compiler (parsing)

• generate a C program for a parser from BNF rules

bison and flex ("fast lex") - more powerful, free versions of
yacc and lex, from GNU Software Fnd'n.



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Classic Parsing Tools

• Lex and Yacc generate C code for your analyzer & parser





Lex Example

```
/* lexer.l */
```

```
lexer.1
8{
                                                 token
#include "header.h"
                                             specification
int lineno = 1;
8}
                                                     lex
မ္မမ္မ
[ \t]* ; /* Ignore whitespace */
                                            lexer.c
n \{ lineno++; \}
[0-9]+ { yylval.val = atoi(yytext);
              return NUMBER; }
[a-zA-Z ][a-zA-Z0-9 ]* { yylval.name = strdup(yytext);
                             return ID; }
\+ { return PLUS; }
- { return MINUS; }
\* { return TIMES; }
\backslash { return DIVIDE; }
= { return EQUALS; }
응응
```

Yacc Example

/* parser.y */

```
parser.y
8{
                                                grammar
#include "header.h"
                                             specification
8}
%union {
                                                    yacc
        char *name;
        int val;
                                            parser.c
%token PLUS MINUS TIMES DIVIDE EQUALS
%token<name> ID;
%token<val> NUMBER;
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start : ID EQUALS expr;
expr : expr PLUS term
          expr MINUS term
          term
        ;
. . .
```



- PLY: Python Lex-Yacc = an implementation of lex and yacc parsing tools for Python by David Beazley: <u>http://www.dabeaz.com/ply/</u>
- A bit of history:
 - Yacc : ~1973. Stephen Johnson (AT&T)
 - Lex : ~1974. Eric Schmidt and Mike Lesk (AT&T)

• PLY: 2001

- PLY is not a code generator
- PLY consists of two Python modules ply.lex = A module for writing lexers Tokens specified using regular expressions Provides functions for reading input text ply.yacc = A module for writing grammars
 You simply import the modules to use them
 - The grammar must be in a file



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```
ΡΙΥ
                                                    token information
      import ply.yacc as yacc
                                                   imported from lexer
      import mylexer
                                            # Import lexer information
      tokens = mylexer.tokens
                                            # Need token list
                                                    grammar rules encoded
      def p assign(p):
                                                    as functions with names
            '''assign : NAME EQUALS expr'''
                                                        p rulename
      def p expr(p):
            '''expr : expr PLUS term
                                              docstrings contain
                                               grammar rules
                      expr MINUS term
                                                 from BNF
                    | term'''
      def p term(p):
            '''term : term TIMES factor
                     term DIVIDE factor
                      factor'''
      def p factor(p):
            '''factor : NUMBER'''
      yacc.yacc() # Build the parser
      data = "x = 3*4+5*6"
      yacc.parse(data) # Parse some text
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```

Parameter p contains grammar symbol values
 def p_factor(p):
 `factor : NUMBER'
 p[0] = p[1]

• PLY does Bottom-up parsing

- Rule functions process values on <u>right hand side</u> of grammar rule
- Result is then stored in left hand side
- Results propagate up through the grammar

```
PLY Calculator Example
          def p assign(p):
              "'assign : NAME EQUALS expr''
              vars[p[1]] = p[3]
          def p_expr_plus(p):
              "'expr : expr PLUS term''
              p[0] = p[1] + p[3]
          def p_term_mul(p):
              ''term : term TIMES factor''
              p[0] = p[1] * p[3]
          def p_term_factor(p):
              '''term : factor'''
              p[0] = p[1]
          def p factor(p):
              '''factor : NUMBER'''
              p[0] = p[1]
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```

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```
Build a parse tree using tuples
            def p assign(p):
                "'assign : NAME EQUALS expr''
               p[0] = ('ASSIGN', p[1], p[3])
            def p_expr_plus(p):
                "'expr : expr PLUS term'"
               p[0] = ('+', p[1], p[3])
            def p_term_mul(p):
                ''term : term TIMES factor'''
               p[0] = ('*', p[1], p[3])
            def p_term_factor(p):
                '''term : factor'''
               p[0] = p[1]
            def p_factor(p):
                '''factor : NUMBER'''
               p[0] = ('NUM', p[1])
```

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```
PLY Precedence Specifiers
• Precedence Specifiers (most precedence at bottom):
     precedence = (
          ('left','PLUS','MINUS'),
          ('left','TIMES','DIVIDE'),
          ('nonassoc', 'UMINUS'),
     def p expr uminus(p):
          'expr : MINUS expr %prec UMINUS'
          p[0] = -p[1]
```

PLY Best Documentation

• Google Mailing list/group:

http://groups.google.com/group/ply-hack

TPG

• TGP is a lexical and syntactic parser generator for Python

- YACC is too complex to use in simple cases (calculators, configuration files, small programming languages, ...)
- You can also add Python code directly into grammar rules and build abstract syntax trees while parsing

Python TPG Lexer

- Toy Parser Generator (TPG): <u>http://cdsoft.fr/tpg</u>
 - Syntax:

token <name> <regex> <function> ;
separator <name> <regex>;

• Example:

token integer '\d+' int; token float '\d+\.\d*|\.\d+' float;

token rbrace '{';

separator space '\s+';

Python TPG Lexer

• Embed TPG in Python:

import tpg

class Calc:

```
r"""
```

separator spaces: '\s+' ;
token number: '\d+' ;
token add: '[+-]' ;
token mul: '[*/]' ;

Try it in Python: download TGP from http://cdsoft.fr/tpg

TPG example

• Defining the grammar:

• Non-terminal productions:

START -> Expr ;

Expr -> Term (add Term)* ;

Term -> Fact (mul Fact)* ;

Fact -> number | '\(' Expr ')' ;

```
TPG example
  import tpg
  class Calc:
   r"""
   separator spaces: '\s+' ;
   token number: '\d+' ;
   token add: '[+-]' ;
   token mul: '[*/]' ;
   START \rightarrow Expr ;
   Expr -> Term ( add Term )* ;
   Term -> Fact ( mul Fact )* ;
   Fact -> number | ' (' Expr ' )' ;
   ** ** **
```

TPG example

• Reading the input and returning values: separator spaces: '\s+' ; token number: '\d+' int ; token add: '[+-]' make op; token mul: '[*/]' make op; • Transform tokens into defined operations: def make op(s): return { '+': lambda x,y: x+y, '-': lambda x,y: x-y, '*': lambda x,y: x*y, '/': lambda x,y: x/y, }[s]

TPG example

- After a terminal symbol is recognized we will store it in a Python variable: for example to save a number in a variable n: number/n.
- Include Python code example:
 Expr/t -> Term/t (add/op Term/f \$t=op(t,f)\$)* ;
 Term/f -> Fact/f (mul/op Fact/a \$f=op(f,a)\$)* ;
 Fact/a -> number/a | '\(' Expr/a '\)' ;

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```
import math
import operator
import string
import tpg
def make op(s):
        return {
                '+': lambda x,y: x+y,
                '-': lambda x,y: x-y,
                '*': lambda x,y: x*y,
                '/': lambda x,y: x/y,
        }[s]
class Calc(tpg.Parser):
        r"""
        separator spaces: '\s+' ;
        token number: '\d+' int ;
        token add: '[+-]' make op ;
        token mul: '[*/]' make op ;
        START/e -> Term/e ;
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```

Simple calculator calc.py

```
Term/t -> Fact/t ( add/op Fact/f $ t = op(t,f) $ )* ;
Fact/f -> Atom/f ( mul/op Atom/a $ f = op(f,a) $ )* ;
Atom/a -> number/a | '\(' Term/a '\)' ;
"""
```

calc = Calc()

```
if tpg.__python__ == 3:
    operator.div = operator.truediv
    raw input = input
```

```
expr = raw_input('Enter an expression: ')
print(expr, '=', calc(expr))
```

```
#!/usr/bin/env python
# Larger example: scientific calc.py
import math
import operator
import string
import tpg
if tpg.__python__ == 3:
     operator.div = operator.truediv
     raw input = input
def make op(op):
     return {
         '+'
                : operator.add,
          ' _ '
                : operator.sub,
          1 🗶 1
                : operator.mul,
         1/1
                : operator.div,
         181
                : operator.mod,
          1 ^ 1
                : lambda x,y:x**y,
         ·** ·
                : lambda x,y:x**y,
         'cos' : math.cos,
         'sin' : math.sin,
         'tan' : math.tan,
         'acos': math.acos, (c) Paul Fodor (CS Stony Brook) and Elsevier
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```

```
'asin': math.asin,
       'atan': math.atan,
       'sqr' : lambda x:x*x,
       'sqrt': math.sqrt,
       'abs' : abs,
       'norm': lambda x,y:math.sqrt(x*x+y*y),
   }[op]
class Calc(tpg.Parser, dict):
   r"""
       separator space '\s+';
       token add op '[+-]' $ make op
       token mul op '[*/%]' $ make op
       token funct1 '(cos|sin|tan|acos|asin|atan|sqr|sqrt|abs)\b' $ make op
       token funct2 '(norm)\b' $ make op
       token real
                     '(\d+\.\d*|\d*\.\d+)([eE][-+]?\d+)?|\d+[eE][-+]?\d+'
               $ float
       token integer '\d+' $ int
       token VarId '[a-zA-Z]\w*'
       ;
```

```
START/e ->
                               $ e=self.mem()
        'vars'
       VarId/v '=' Expr/e $ self[v]=e
    Expr/e
    ;
Var/$self.get(v,0)$ -> VarId/v ;
Expr/e -> Term/e ( add_op/op Term/t  $ e=op(e,t)
                ) *
;
Term/t -> Fact/t ( mul_op/op Fact/f $ t=op(t,f)
                ) *
;
Fact/f ->
       add op/op Fact/f
                                       f = 00(0, f)
       Pow/f
    L
;
Pow/f -> Atom/f ( pow op/op Fact/e $ f=op(f,e)
                )?
;
```
```
Atom/a ->
           real/a
           integer/a
        Function/a
        Var/a
        1
          '\(' Expr/a '\)'
    ;
   Function/y ->
           funct1/f '\(' Expr/x '\)'
                                              y = f(x)
        | funct2/f '\(' Expr/x1 ',' Expr/x2 '\)' $ y = f(x1,x2)
11 11 11
def mem(self):
   vars = sorted(self.items())
   memory = [ "%s = %s"%(var, val) for (var, val) in vars ]
   return "\n\t" + "\n\t".join(memory)
```

```
print("Calc (TPG example)")
calc = Calc()
while 1:
    l = raw_input("\n:")
    if 1:
        try:
        print(calc(l))
```

except Exception:

print(tpg.exc())

else:

break



(c) Paul Fodor (CS Stony Brook) and Elsevier

AntLR

ANother Tool for Language Recognition is an LL(k) parser and translator generator tool which can create

- lexers
- parsers
- abstract syntax trees (AST's)

in which you describe the language grammatically and in return receive a program that can recognize and translate that language

Tasks Divided

- Lexical Analysis (scanning)
- Semantic Analysis (parsing)
- Tree Generation
- Abstract Syntax Tree (AST) is a structure which keeps information in an easily traversable form (such as operator at a node, operands at children of the node)
 ignores form-dependent superficial details
 Code Generation

The Java Code

```
• The code to invoke the parser:
import java.io.*;
class Main {
  public static void main(String[] args) {
   try {
      // use DataInputStream to grab bytes
      MyLexer lexer = new MyLexer(
            new DataInputStream(System.in));
      MyParser parser = new MyParser(lexer);
      int x = parser.expr();
      System.out.println(x);
    } catch(Exception e) {
      System.err.println("exception: "+e);
```

Abstract Syntax Trees

- Abstract Syntax Tree: Like a parse tree, without unnecessary information
- Two-dimensional trees that can encode the structure of the input as well as the input symbols
- An AST for (3+4) might be represented as



• No parentheses are included in the tree!