

**Q1. Fractional Knapsack using SELECT**

We walk in to a store with a budget  $B$ . The store has  $N$  types of items each with  $m_i$  number of units. For each item type  $i$  in the store, the unit cost of the item  $i$  is  $c_i$  and unit value of the item  $i$  is  $v_i$ . Any fraction  $f$  of the types of items can be purchased, where  $0 \leq f \leq m_i$ . For fraction  $f$  the cost is  $f \times c_i$  and the value is  $f \times v_i$ .

We want to select all or portion of the items of each type in the store so as to maximize the value without exceeding the budget  $B$ . Describe an efficient algorithm to determine what portion of each type of items we should buy. Analyze the time of your algorithm.

\* **Hint:** Utilize the SELECT algorithm. Define a variable that represent efficacy of the unit item in terms of  $c_i$  and  $v_i$ .